

# Epoch reference frames as short-term realizations of the ITRS - recent developments and future challenges -

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# Motivation I

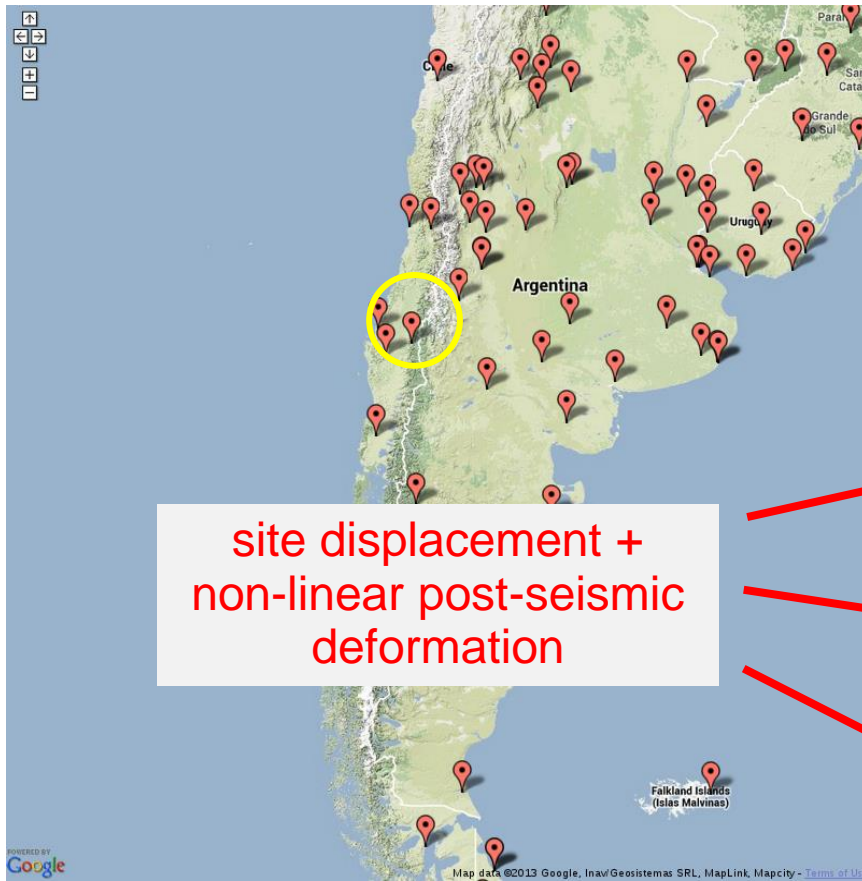
**A precisely defined Terrestrial Reference Frame (TRF) is needed e.g. for quantifying**

- Earth rotation
- Earth gravity field
- atmospheric or hydrologic loading
- global and regional sea level variations
- tectonic motion and crustal deformation
- post-glacial rebound
- geocenter motion
- large scale deformation due to earthquakes
- local subsidence

**and for practical applications such as surveying, engineering, mapping, GIS.**

(Description of Theme 1, IAG 2013  
IAG/IERS JWG 1.4)

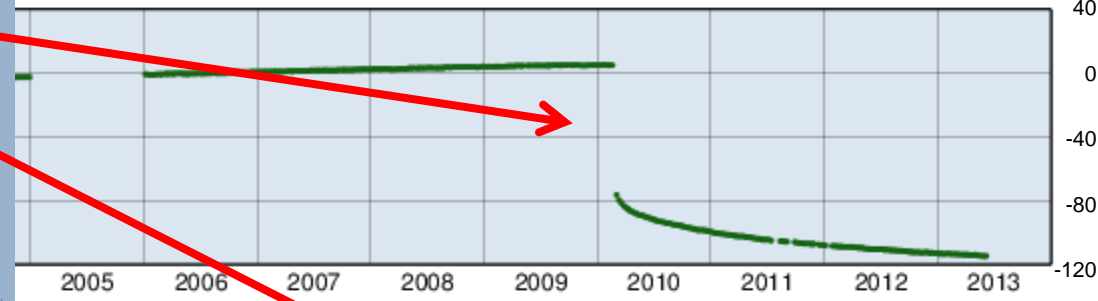
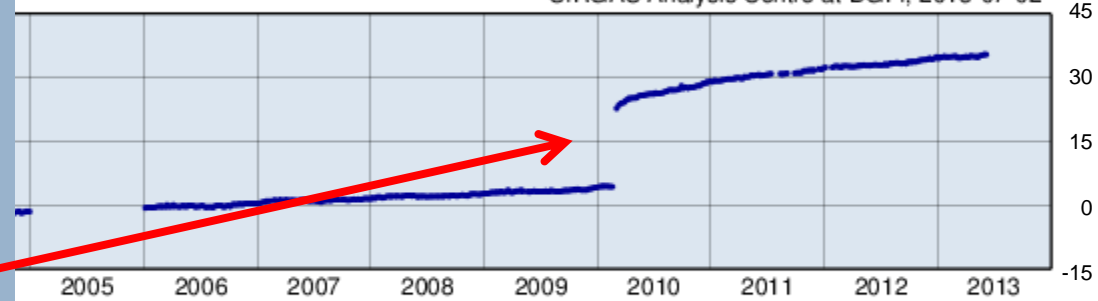
# Motivation II



site displacement +  
non-linear post-seismic  
deformation

Station ANTC

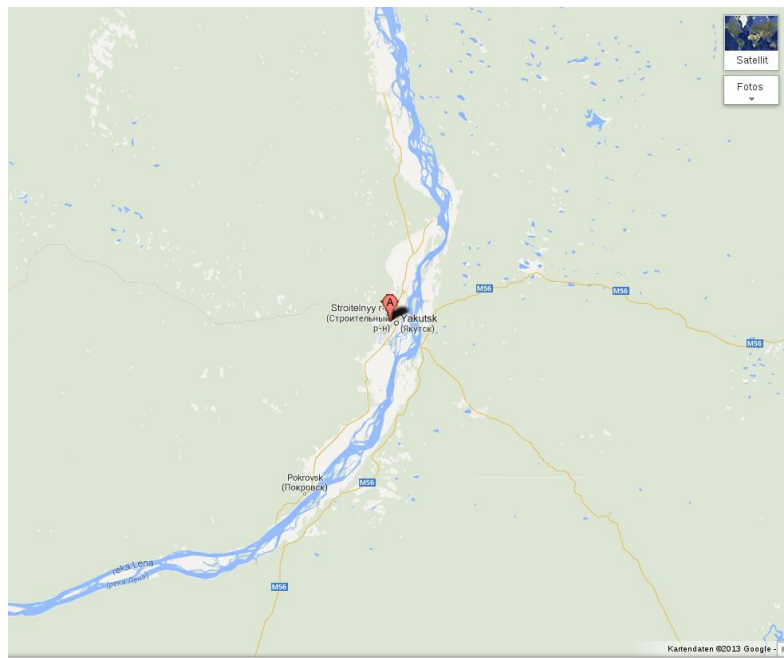
SIRGAS Analysis Centre at DGFI, 2013-07-02 [cm]



UP COMPONENT [cm]

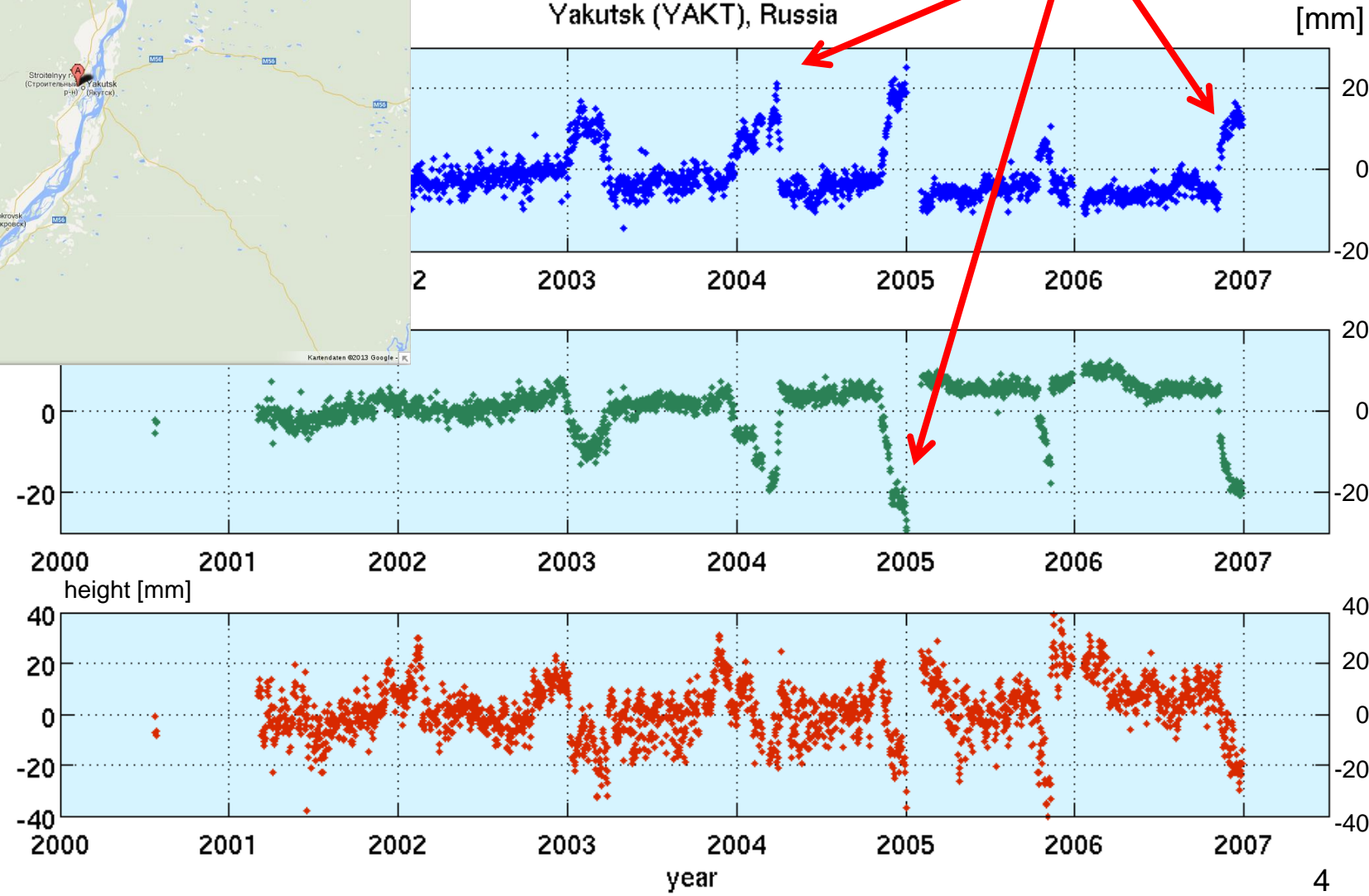


# Motivation II



seasonal site displacement due to e.g. snow cover, river flow rate, ...

Yakutsk (YAKT), Russia



# Treatment of non-linear station motions?

## ➤ Parameterization

- Research Unit “Space-time reference systems for monitoring global change and for precise navigation in space” ([www.referenzsysteme.de](http://www.referenzsysteme.de))



## ➤ Modeling

- IAG/IERS JWG 1.2 “Modeling environmental loading effects for reference frame realizations” (chair: X. Collilieux)
- presentations by T. van Dam and J. Freymueller
- presentations in Theme 1.6



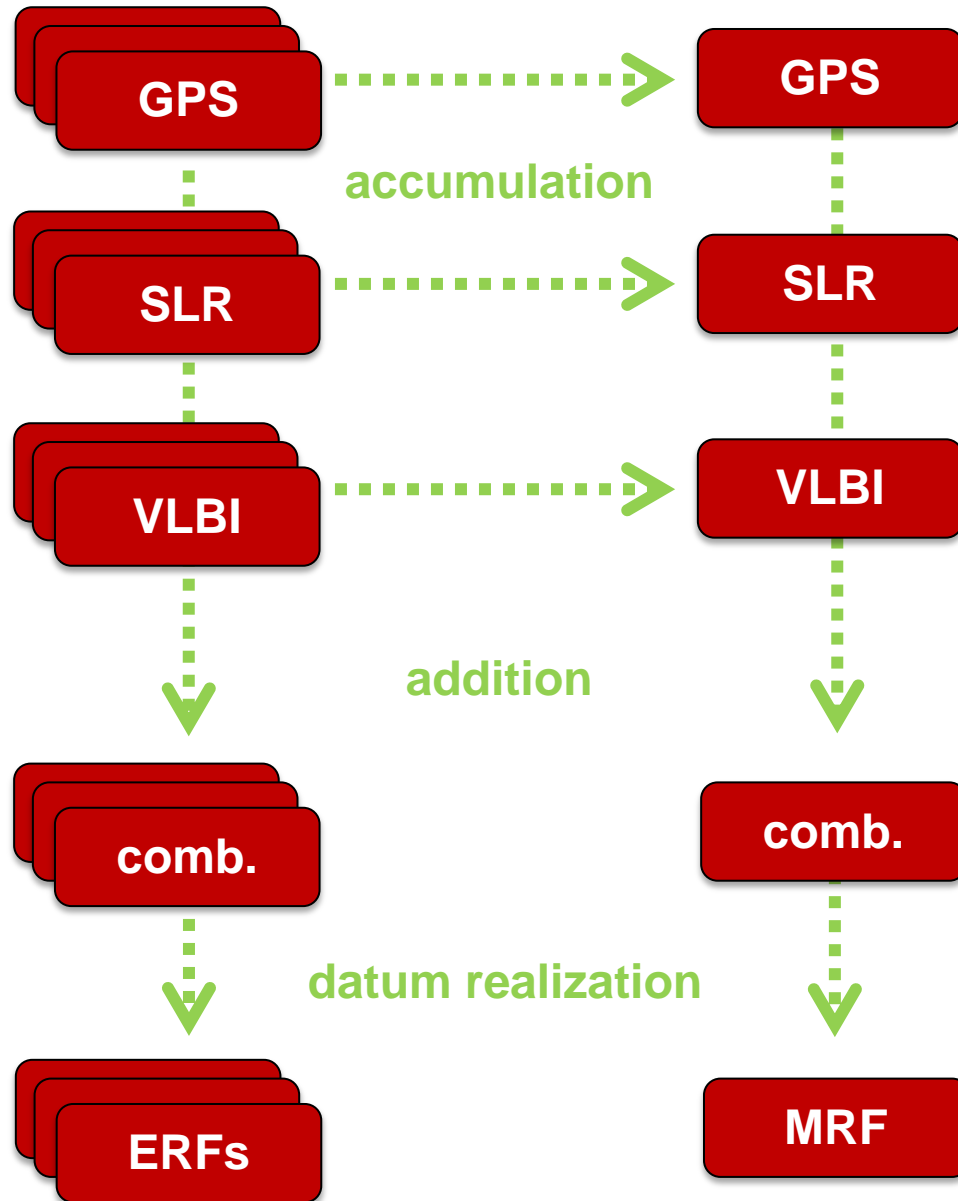
## ➤ Sampling

- IAG/IERS JWG 1.4 “Strategies for epoch reference frames” (chair: M. Seitz)
- this presentation



# Computation scheme

## pre-processing



## pre-processing:

- time series analysis (outliers, discontinuities, parameterization, ...)

## datum realization:

- origin: SLR
- orientation: NNR condition (GPS subnet)
- scale: mean of SLR and VLBI

## Multi-year reference frame (MRF):

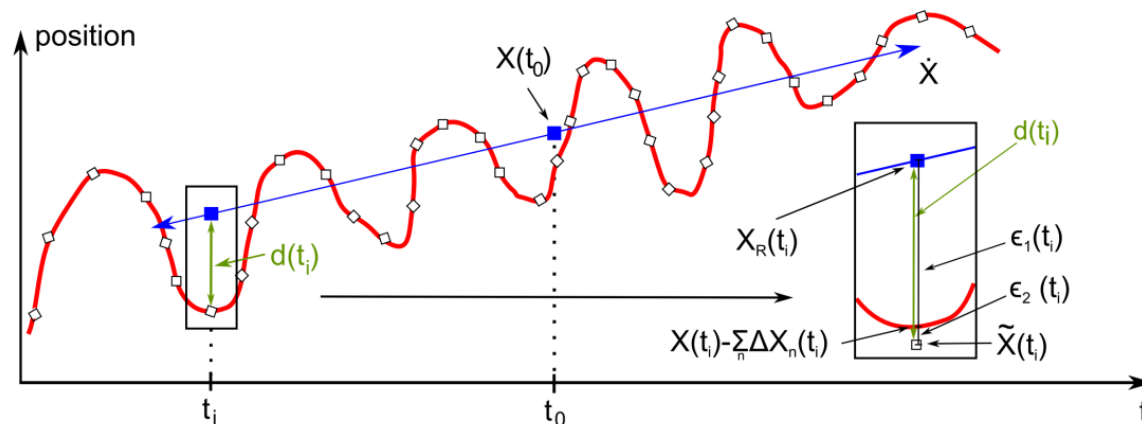
- combined secular TRF (pos+vel+EOP)

## Epoch reference frame (ERF):

- epoch-wise combined TRF (pos+EOP)
- sampling: 7d, 14d, 28d

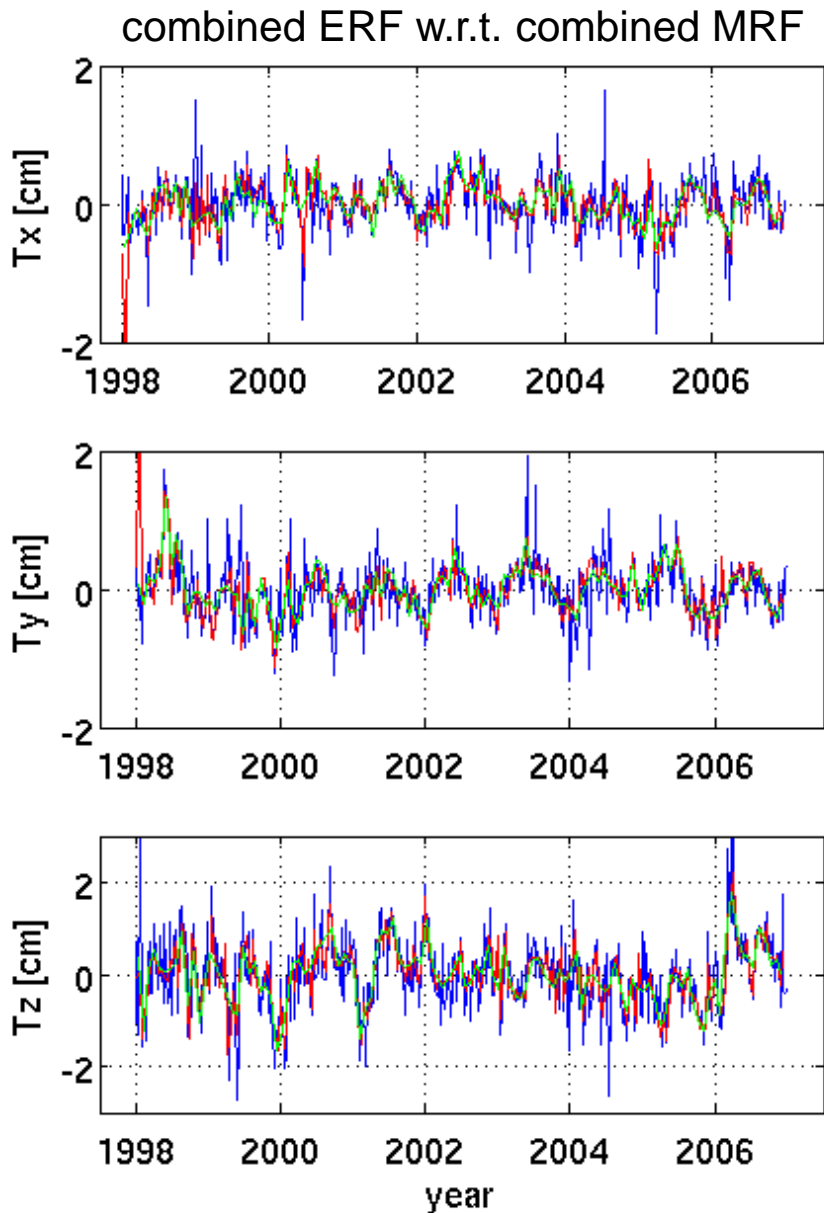
# Sampling of non-linear station motions

- 1<sup>st</sup> Reduction of conventionally modeled effects (e.g. Earth tides, ocean tides)
- 2<sup>nd</sup> Approximation of regularized station position through frequently sampling



- Regularized station motion is dominated by seasonal effects caused by neglected hydrological/atmospheric loading
- Differences between secular and epoch-wise estimation can be split up into
  - common motions of all stations (equal to transformation parameters between ERFs and MRF)
  - individually performed motions of a particular station

# Transformation parameters - Translations

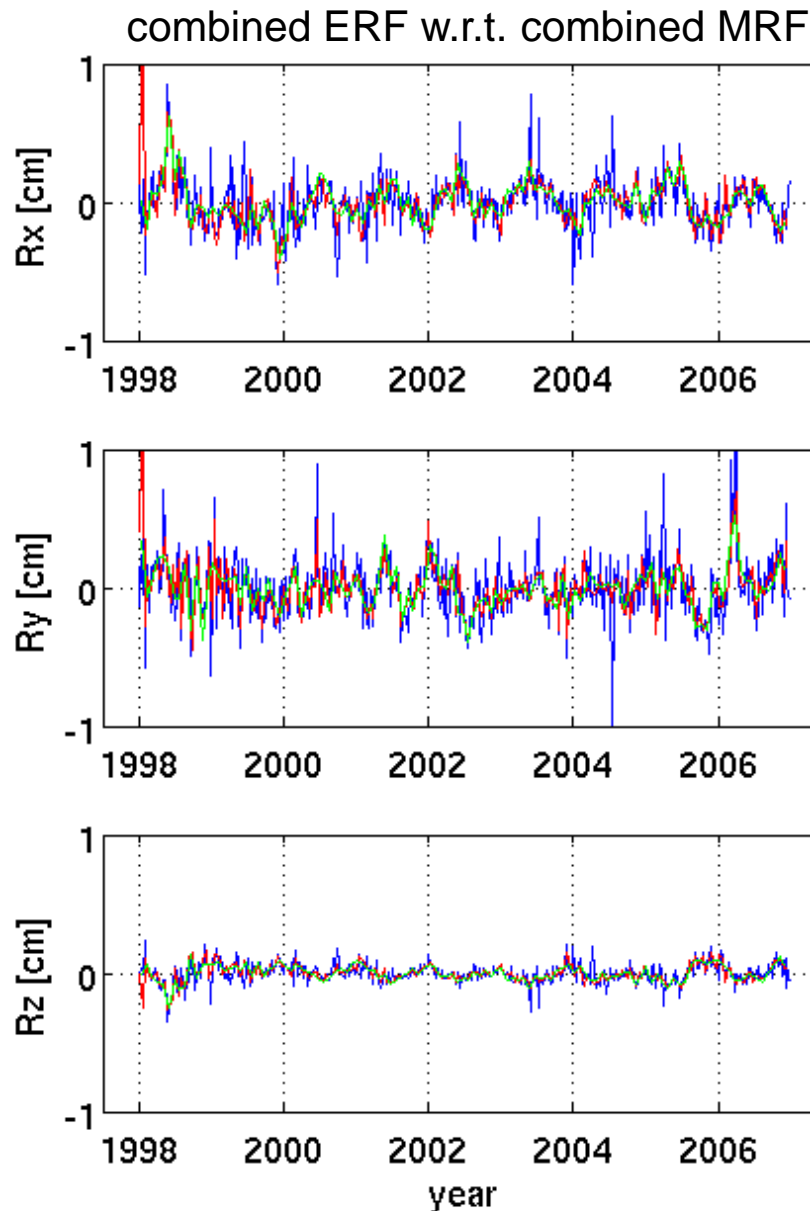


|            | A [mm] | $\Phi$ [days] | RMS[mm] |
|------------|--------|---------------|---------|
| <b>7d</b>  | 1.7    | 193.4         | 4.0     |
| <b>14d</b> | 1.8    | 211.9         | 3.5     |
| <b>28d</b> | 1.9    | 219.0         | 2.8     |
| <b>7d</b>  | 2.7    | 303.7         | 4.8     |
| <b>14d</b> | 2.6    | 304.3         | 4.6     |
| <b>28d</b> | 2.7    | 306.3         | 3.7     |
| <b>7d</b>  | 2.0    | 245.9         | 8.5     |
| <b>14d</b> | 2.2    | 245.9         | 6.9     |
| <b>28d</b> | 2.2    | 257.4         | 6.2     |

- annual amplitudes are independent from sampling interval
- phases in Tx show scatter of 26 days
- RMS is reduced if the sampling interval is enlarged



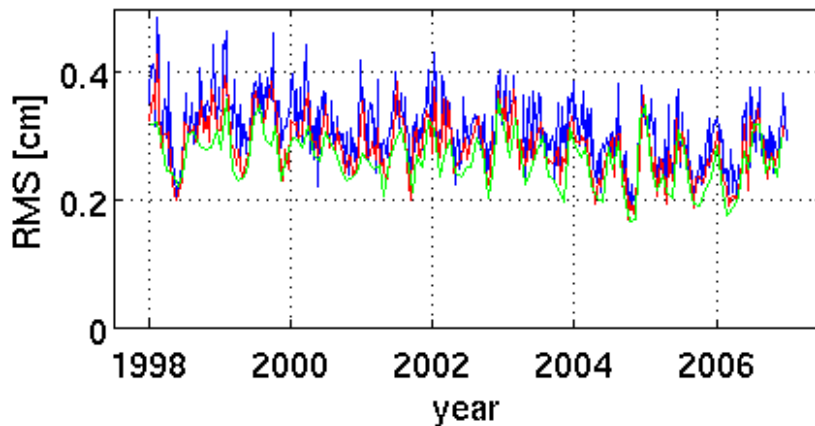
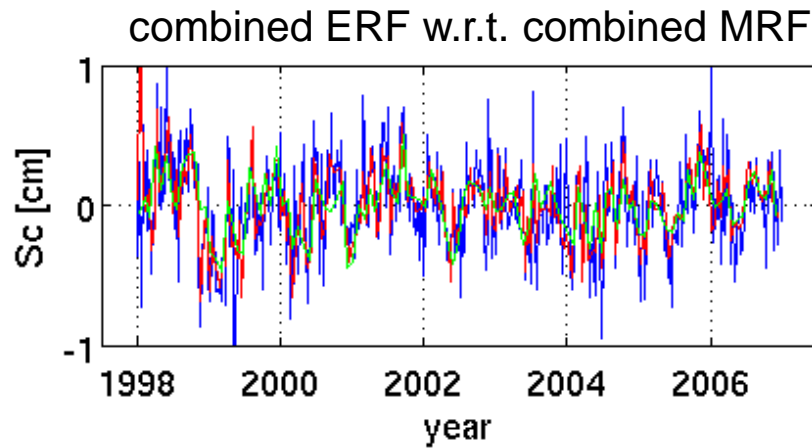
# Rotations



|                  | A [mm] | $\Phi$ [days] | RMS[mm] |     |
|------------------|--------|---------------|---------|-----|
| 7d<br>14d<br>28d | Rx     | 1.1           | 299.6   | 1.9 |
|                  |        | 1.1           | 298.9   | 1.8 |
|                  |        | 1.2           | 302.4   | 1.5 |
| 7d<br>14d<br>28d | Ry     | 0.7           | 356.7   | 2.3 |
|                  |        | 0.6           | 11.0    | 1.9 |
|                  |        | 0.7           | 24.7    | 1.5 |
| 7d<br>14d<br>28d | Rz     | 0.5           | 120.9   | 0.8 |
|                  |        | 0.5           | 119.9   | 0.7 |
|                  |        | 0.5           | 122.4   | 0.6 |

- annual variation in rotations although NNR condition is applied
- correlations of translations and rotations due to sparse station network
- amplitudes do not decrease if the sampling interval is enlarged

# Scale / network deformation

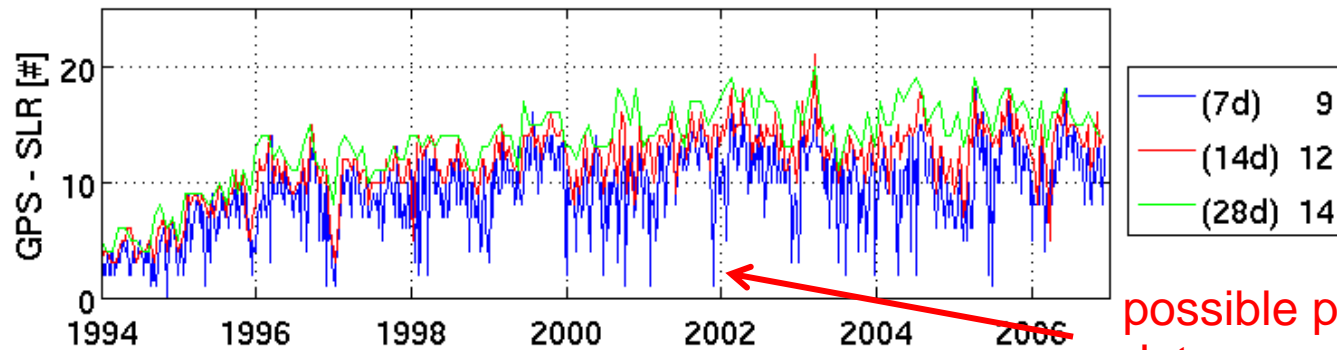
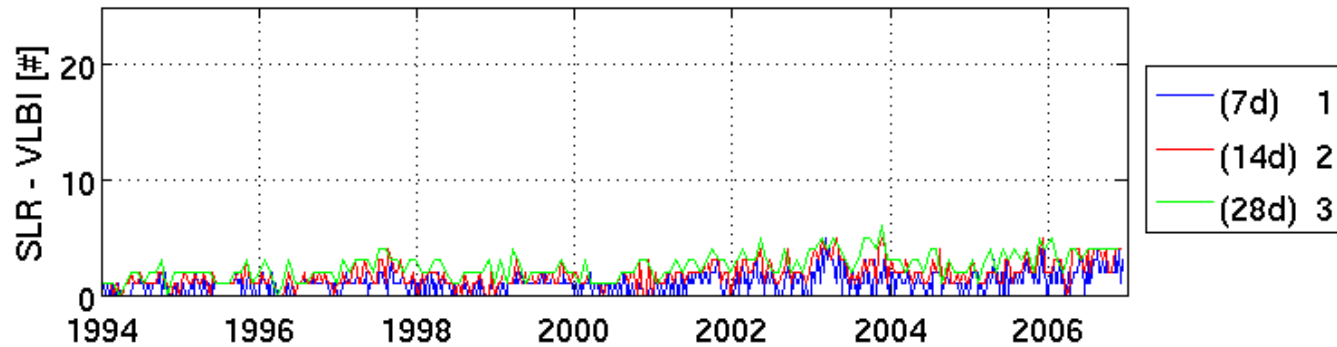


|     | A [mm] | $\Phi$ [days] | RMS[mm] |
|-----|--------|---------------|---------|
| 7d  | 1.1    | 183.3         | 5.0     |
| 14d | 1.0    | 188.2         | 4.8     |
| 28d | 1.2    | 190.8         | 4.4     |

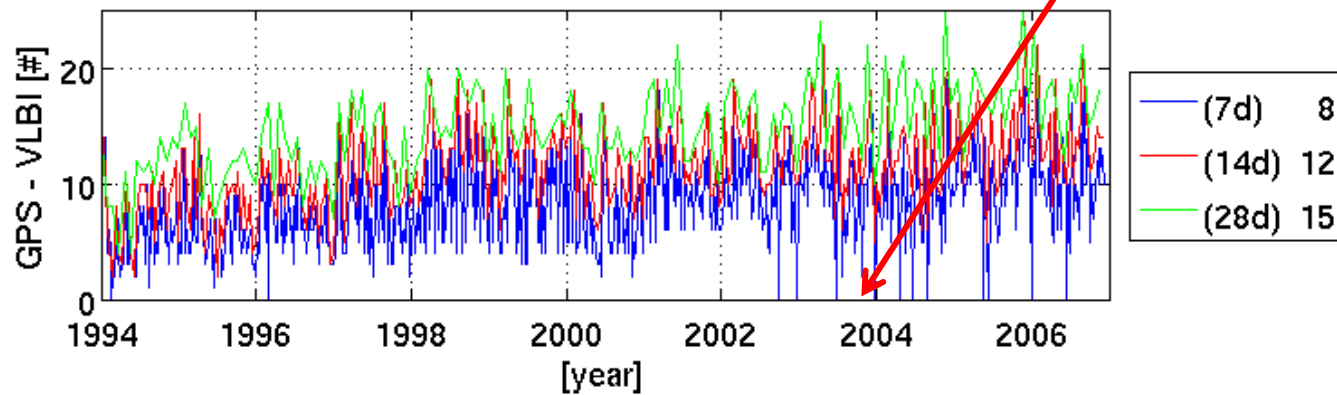
- annual scale variation mainly due to non-modeled loading effects
- amplitudes and phases independent from sampling interval
- mean network deformation decreases with longer sampling interval (7d: 3.1 mm; 28d: 2.6 mm)

➤ The longer the sampling interval is, the more stable is the realized geodetic datum!

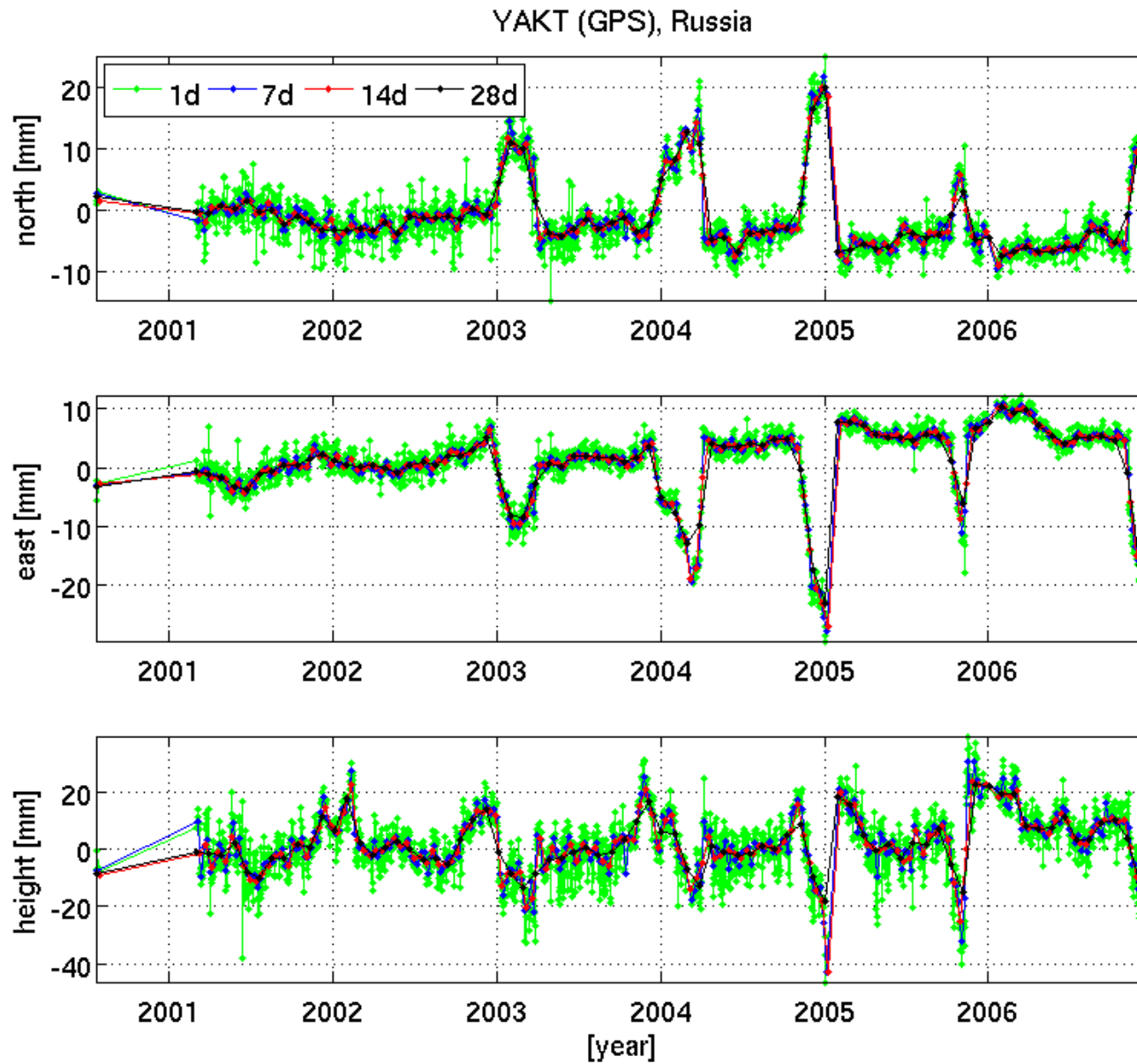
# Number of local ties per epoch



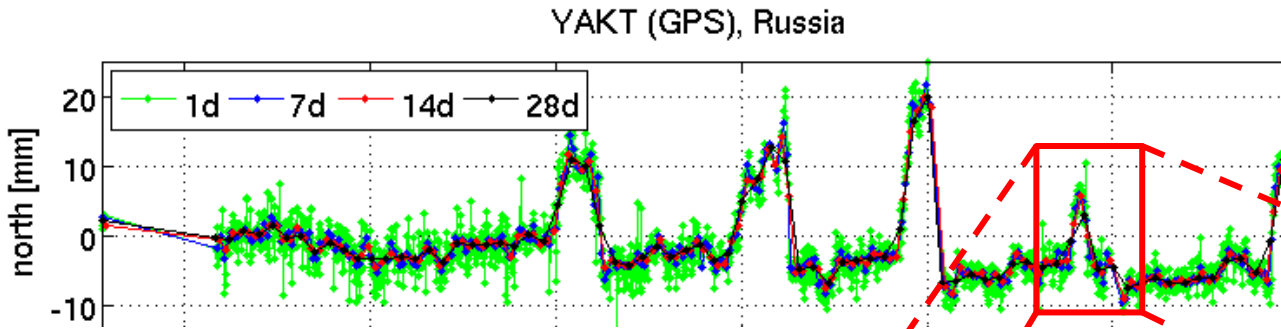
possible problems with datum realization



# Sampling of station motions

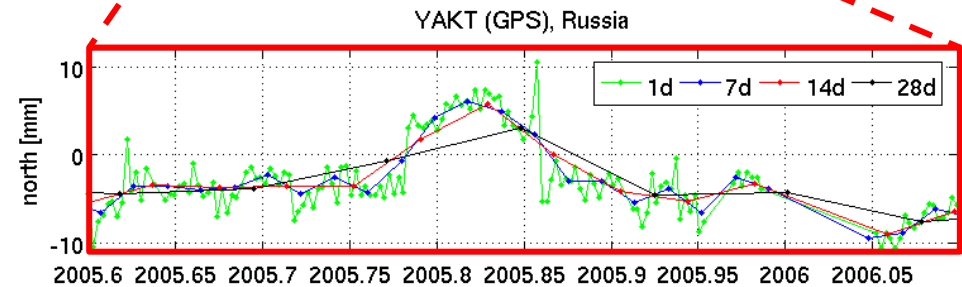


# Sampling of station motions



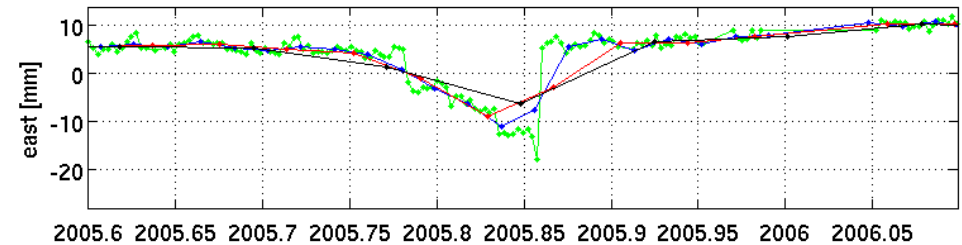
## short-term motions

- with a long sampling interval, short-term motions might not be sampled accurately



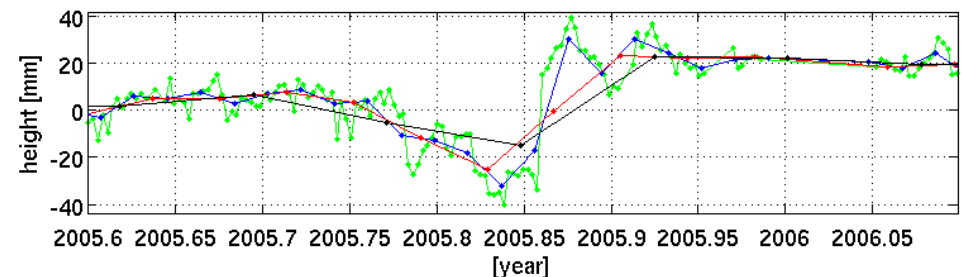
## long-term motions

- long-term motions can be sampled well with 7d, 14d and 28d



## secular motions

- the error of a constant position per epoch increases with the sampling interval (e.g. Easter Island: ca. 6 mm/28d)



# Pros and Cons

|                                    | MRF                     | ERF                 |
|------------------------------------|-------------------------|---------------------|
| stability                          | long-term               | short-term          |
| parameterization                   | $X_R(t_0), \dot{X}$     | $\tilde{X}(t_i)$    |
| estimated positions                | precise (formal errors) | accurate (geometry) |
| position latency after earthquakes | $\geq 2.5$ years        | few epochs          |
| non-linear station motions         | suppressed              | frequently sampled  |
| station network                    | dense                   | sparse              |
| number of LTs                      | high                    | low                 |

- Different applications might need different TRF realizations.

# Summary – Which TRF for which application?

- **Multi-year reference frame (e.g. ITRF2008 / DTRF2008)**
  - parameterization of secular station motions
  - optimal for monitoring long-term changes of the Earth system (e.g. sea level rise, tectonic motion, etc.)
- **Epoch reference frames (e.g. 28-day sampling)**
  - frequently estimated station positions (every 28 days)
  - able to monitor annual variations and post-seismic deformations
  - higher datum stability than 7d / 14d ERFs
  - constant position causes errors up to 3 mm (neglect of secular motion during 28 days)
- **Epoch reference frames (e.g. 7-day / 14-day sampling)**
  - station position estimates every 7 / 14 days
  - able to monitor short-term station motions such as local environmental effects
  - low datum stability due to sparse station networks (especially in the early 90's)

➔ **For the ERFs, we need more dense networks and more colocations with accurately measured local ties.**

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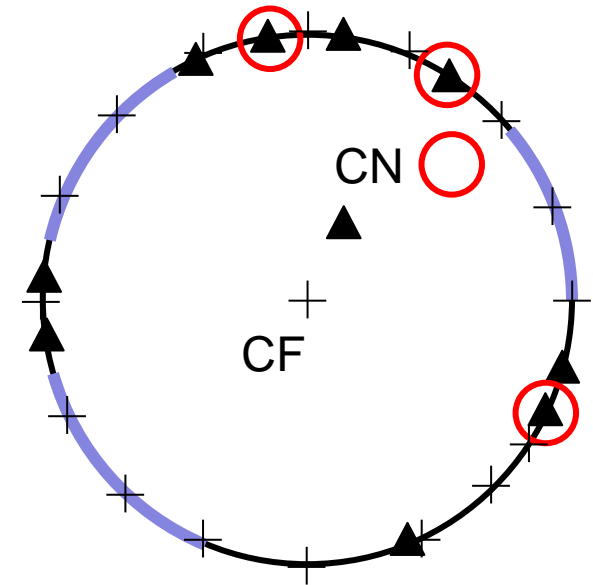
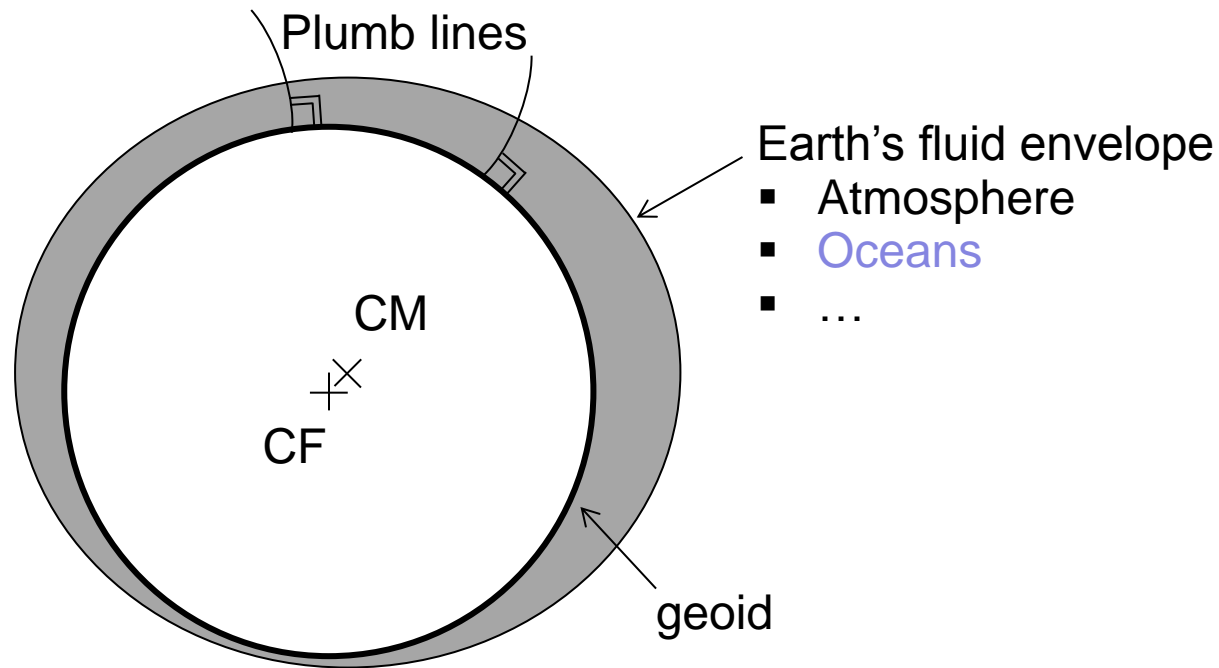
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# TRF origin and center



CM – Center of Mass

CF – Center of Figure

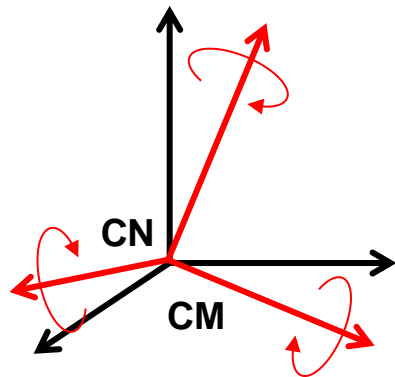
CN – Center of Network (barycenter of network coordinates)

ON – Origin of Network; for SLR/combined TRF: ON = CM

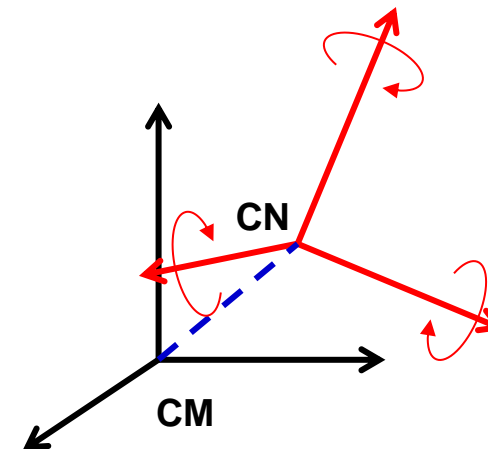
# Geocentric NNR condition

- NNR condition has to be applied w.r.t. **CM** (see position paper to IERS Conventions Workshop 2007 by Petit et al.)
- Since the NNR condition is applied on a subset of station coordinates, the **CN** of this subnet is never equal to the **CM**. The difference between **CM** and **CN** is a common translation of all stations.
- The common translations are correlated with the rotations, if the station network is not well distributed.

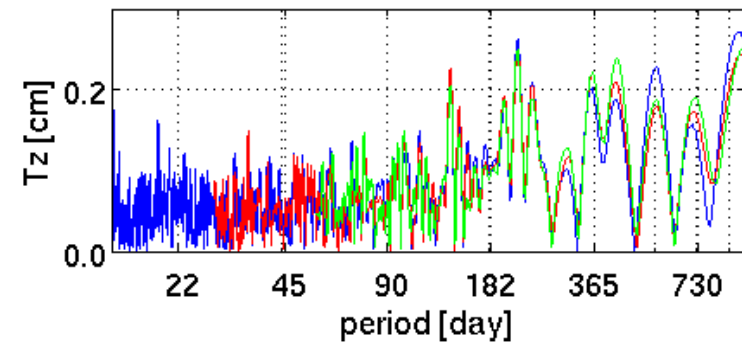
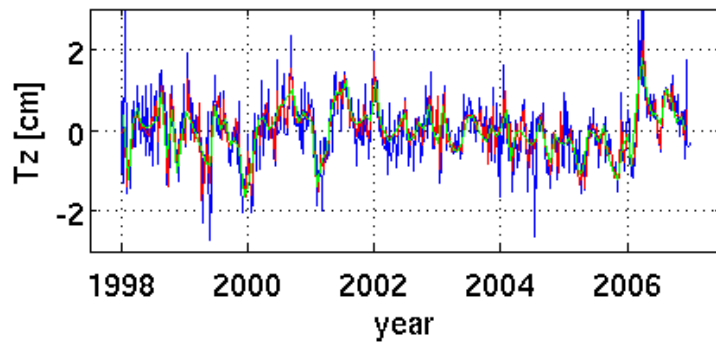
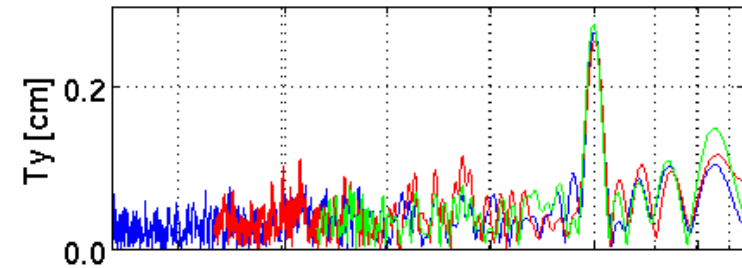
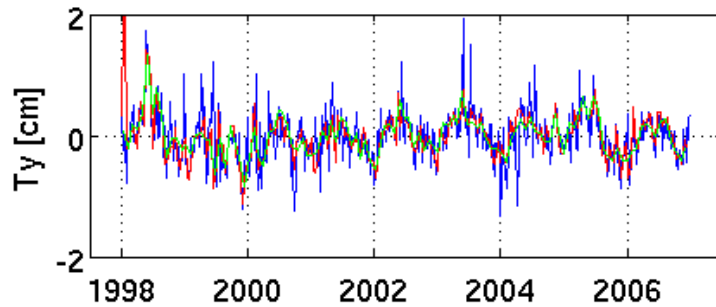
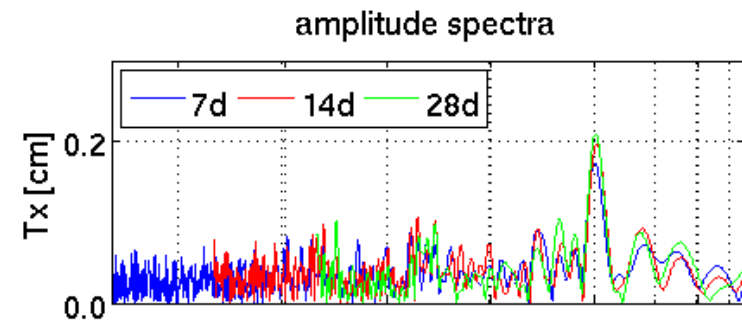
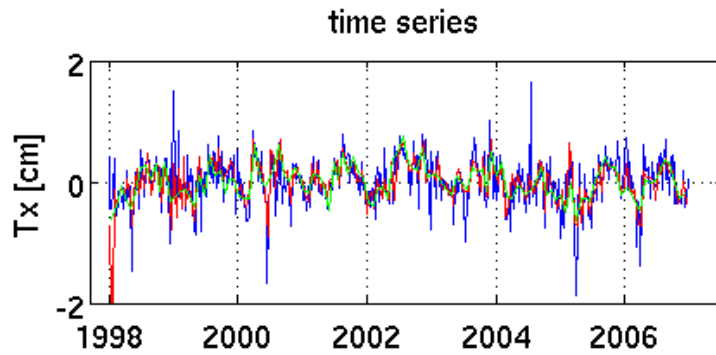
optimal: **CN = CM**



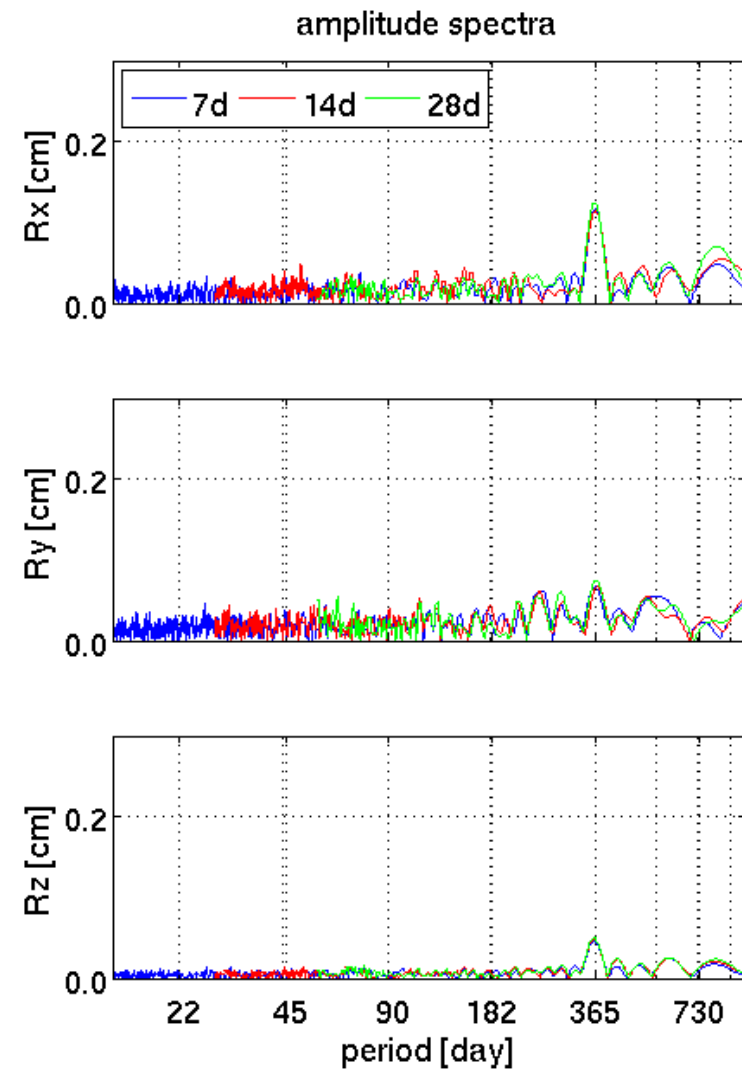
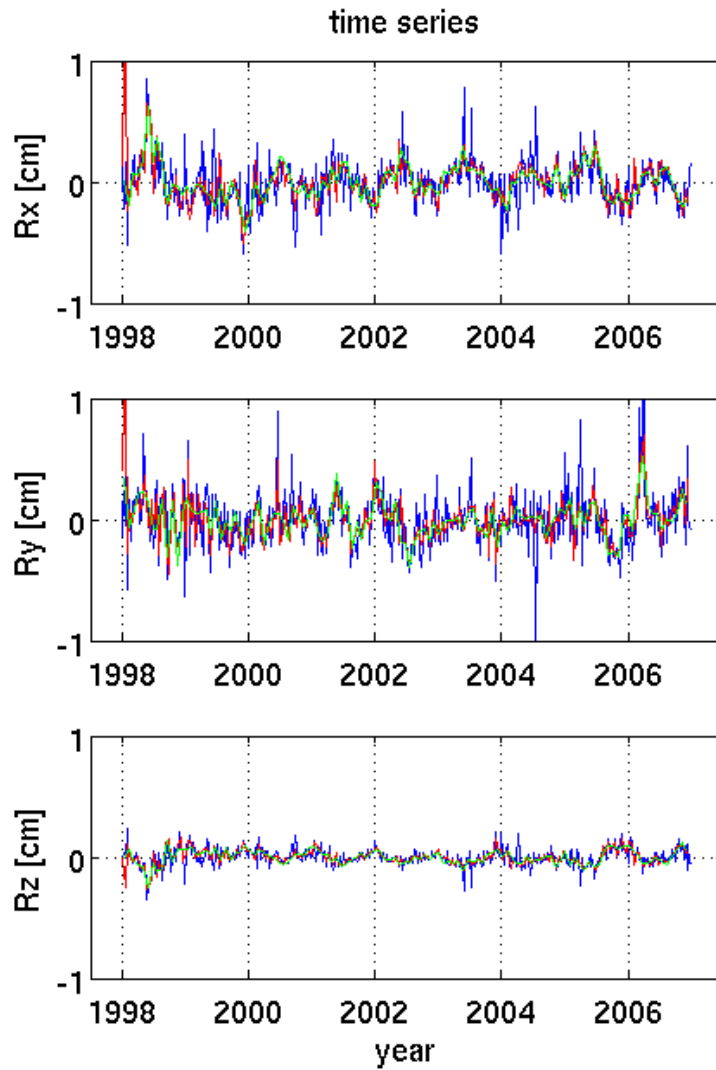
reality: **CN = CM**



# Transformation parameters - Translations



# Rotations



# Scale / network deformation

