



# Interaction between subdaily Earth rotation parameters and GPS orbits

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# Introduction

Subdaily Earth Rotation model: IERS2010 (+ libration)

Kept fixed in the processing

Errors up to ~20%

Empirical tidal models from GPS & VLBI:

Big corrections (more than 10  $\mu\text{as}$  in PM) for some tidal terms:

K1(23.93h), S1 (24h), M2(12.42h), S2(12h), K2(11.97h)

IERS2010+libration: K1 correction ~30  $\mu\text{as}$

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Influence of changes in subdaily model on the orbits, coordinates, ERPs

Influence on the reference frames realized by the satellites

# Data and solutions

## Data:

Daily NEQs (1994-2007): station coordinates, 1h-ERPs, GPS orbits

IERS2000 subdaily model used in processing

## What we do:

Daily solutions, transformation 1h-ERPs → tidal terms

change a priori values for tidal terms + fix tidal terms

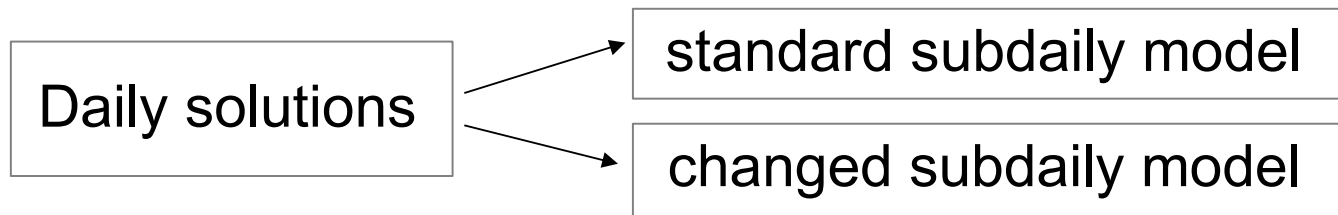
→ change subdaily model

## Daily estimates:

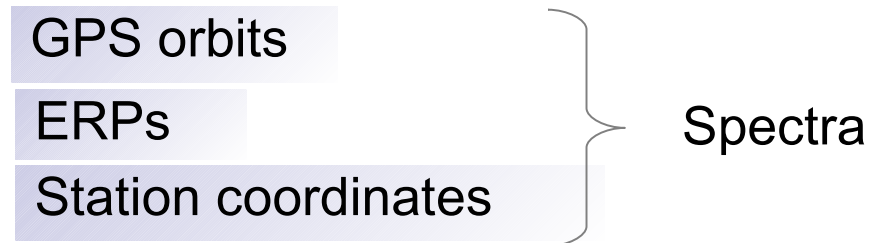
GPS orbits, station coordinates, geocenter (NNR+NNT), 24h ERPs

# Data and solutions

Influence of subdaily tidal model: change 1 tide in PM by  $\sim 100 \mu\text{as}$



Time series of differences:

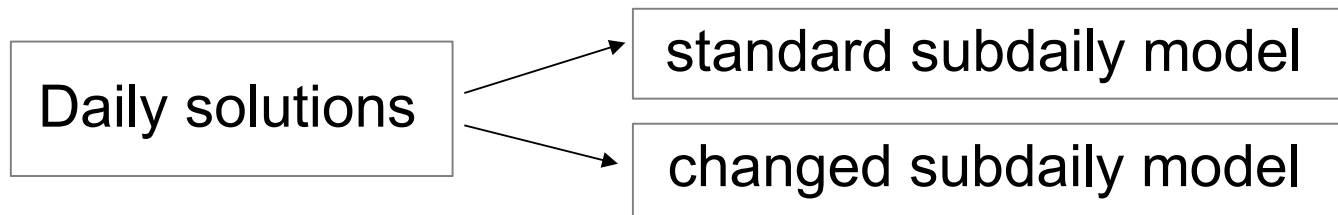


Systematic differences in reference frames realized by orbits:

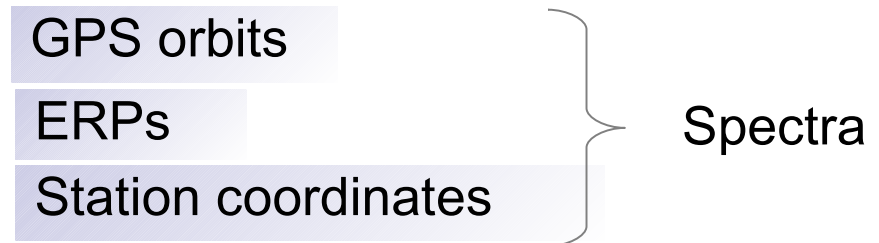
Helmert parameters between standard and changed orbits

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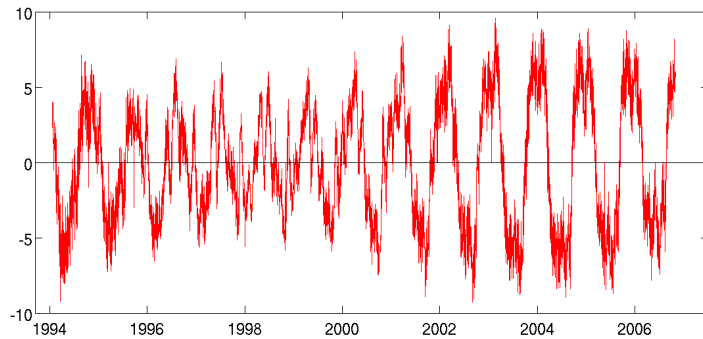


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# Helmert parameters between standard orbit and changed orbit

GPS orbits computed with standard subdaily model vs  
subdaily model with changed S1 tide in PM

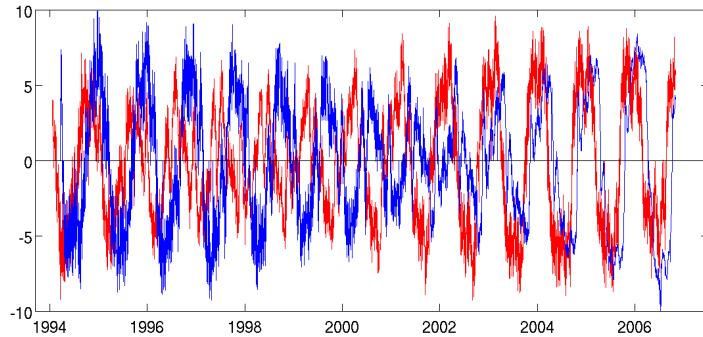


X translation: PRN5



# Helmert parameters between standard orbit and changed orbit

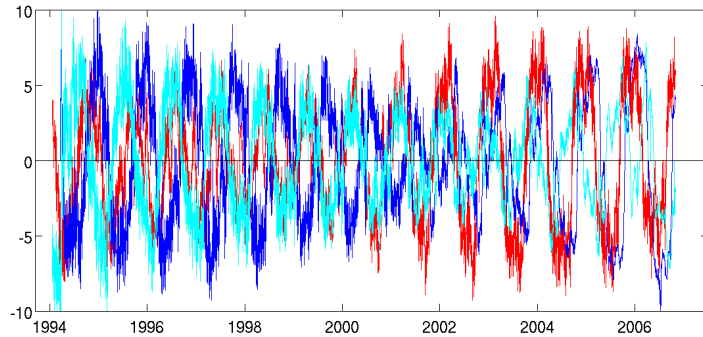
GPS orbits computed with standard subdaily model vs  
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X translation: PRN5, PRN6

# Helmert parameters between standard orbit and changed orbit

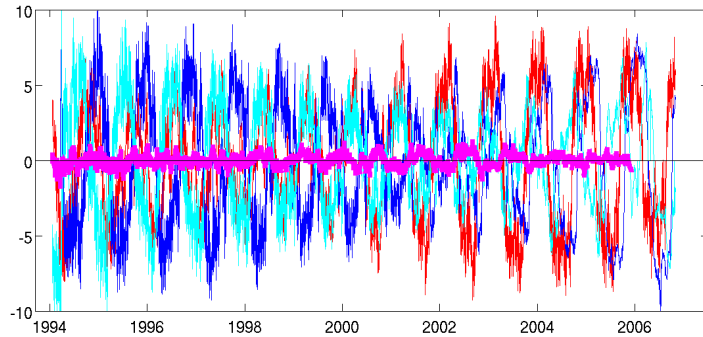
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X translation: PRN5, PRN6, PRN7

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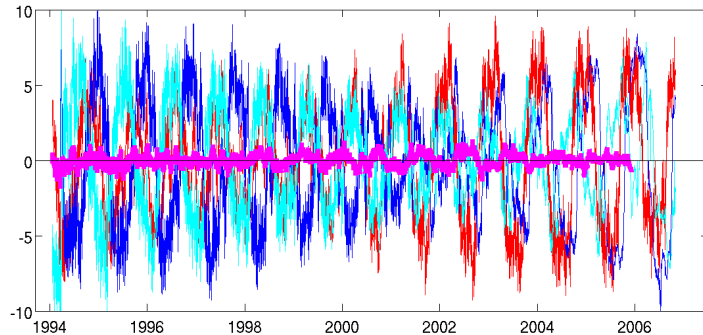
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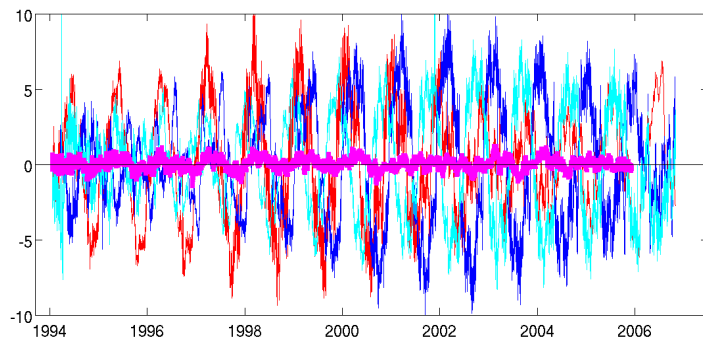
X translation: PRN5, PRN6, PRN7,  
all satellites

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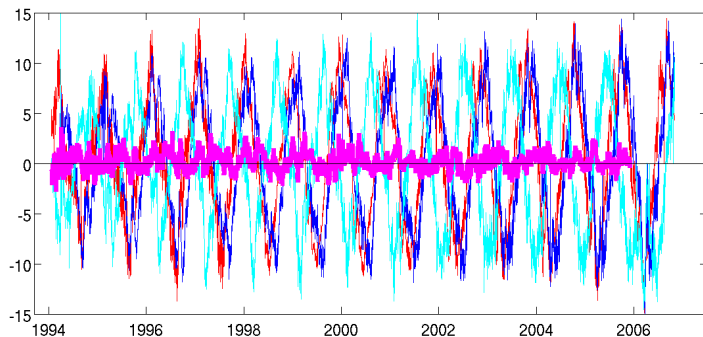
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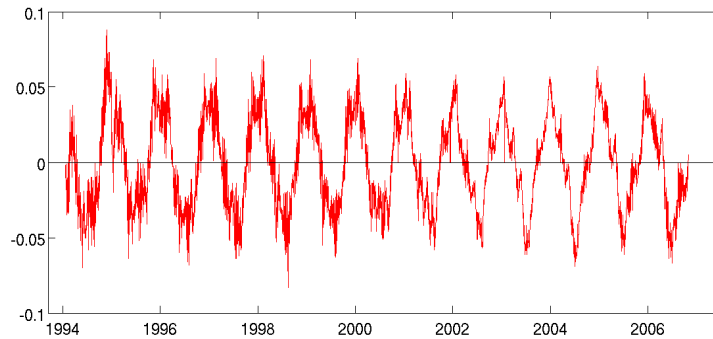
Y translation: PRN5, PRN6, PRN7,  
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Z translation: PRN5, PRN6, PRN7,  
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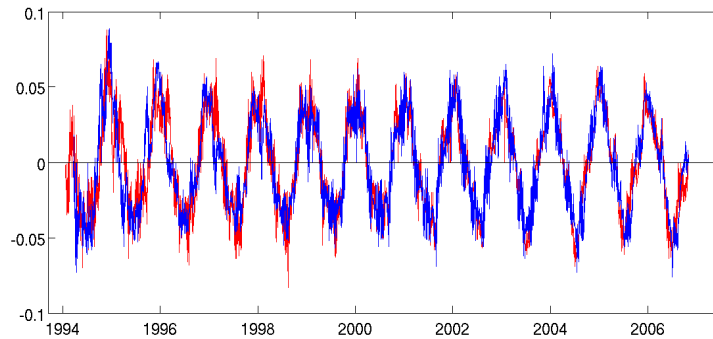
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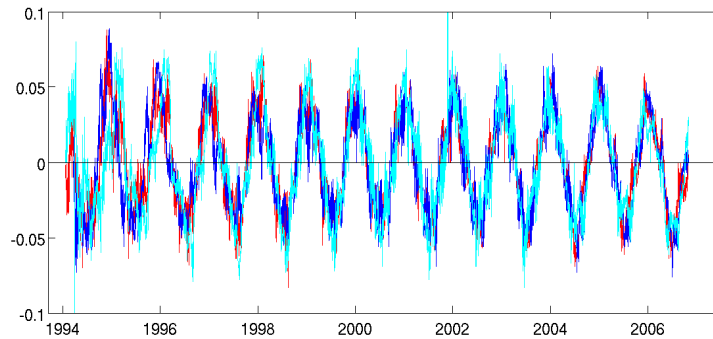
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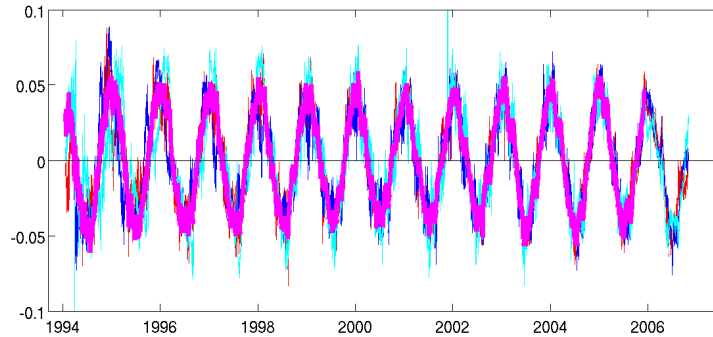
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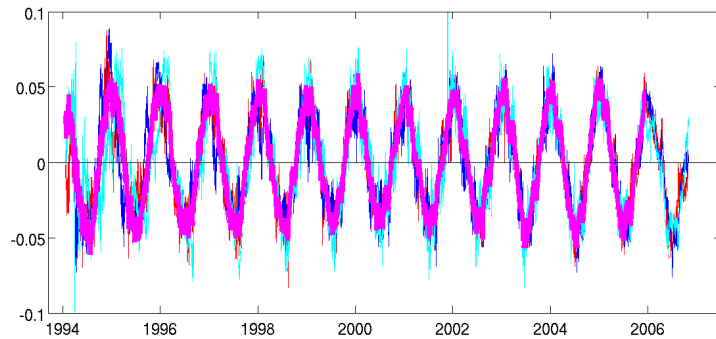


X rotation: PRN5, PRN6, PRN7,  
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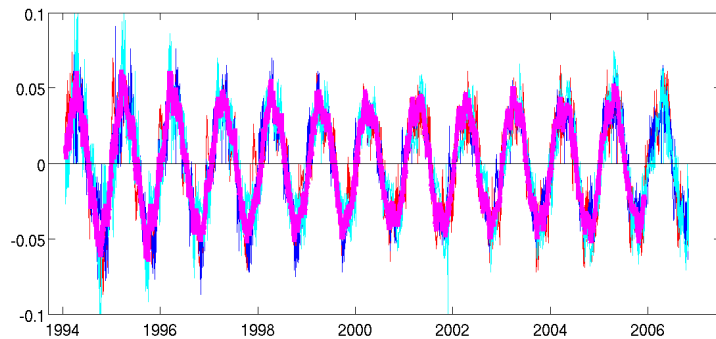


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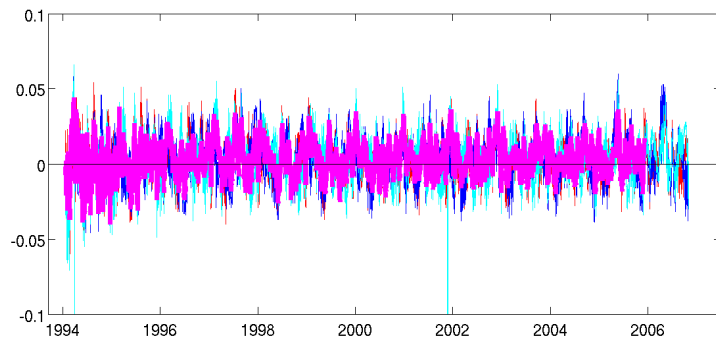
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X rotation: PRN5, PRN6, PRN7  
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## Changes in the subdaily tidal model:

No influence on the origin of the satellite reference frame

Changes in orientation: common rotation of the whole satellite constellation

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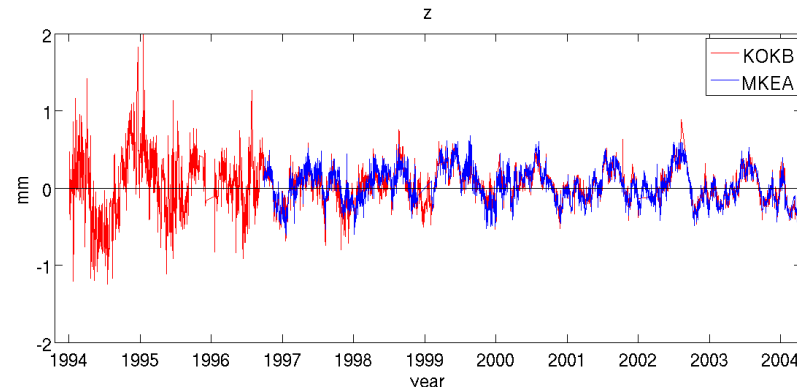
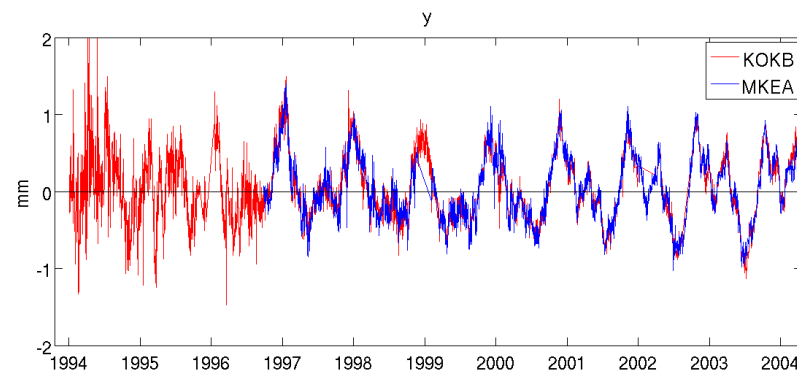
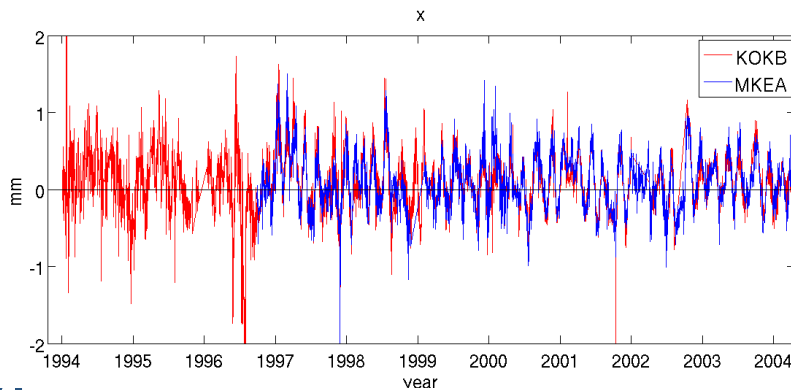
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Changes in orientation: **common rotation** of the whole satellite constellation



Changes in station coordinates caused by changed S1 tide in subdaily model:

stations KOKB, MKEA (Hawaii)



# Subdaily model for ERPs

IERS2010 model for subdaily ERPs contains in PM:

Prograde diurnal terms

Prograde and retrograde semi-diurnal terms

No retrograde diurnal terms



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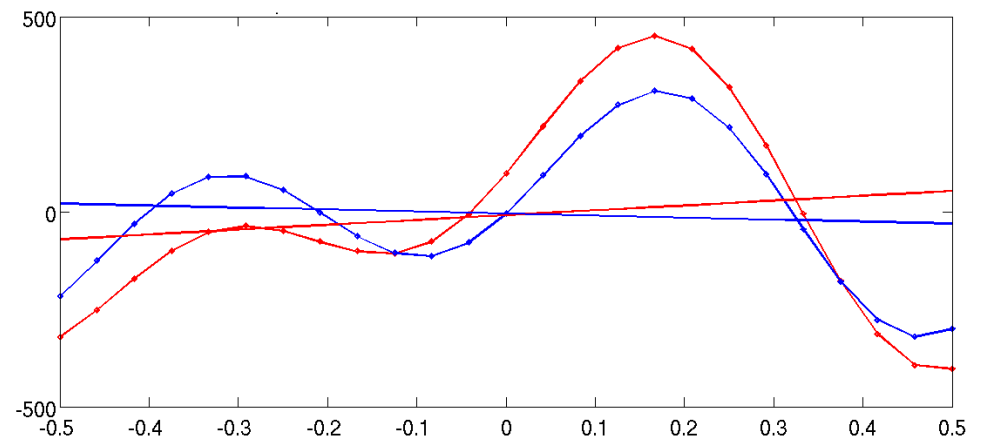
Prograde and retrograde semi-diurnal terms

No retrograde diurnal terms



Modelled ERPs over one day:

Standard model and  
model with changed S1 tide



# Subdaily model for ERPs

Modelled ERPs with 1h resolution over 1994-2007:

Standard subdaily model

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Time series of ERPs computed from standard model:

For each day: fit by LSE retrograde diurnal wave

→ (1) amplitudes of sine and cosine



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Time series of ERPs computed from model with changed S1:

For each day: fit by LSE retrograde diurnal wave

→ (2) amplitudes of sine and cosine

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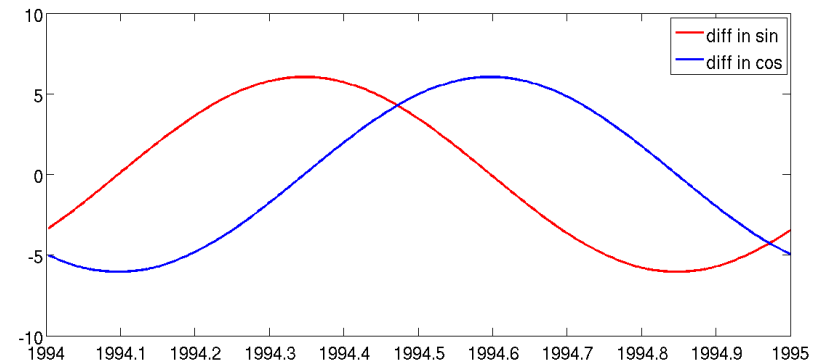
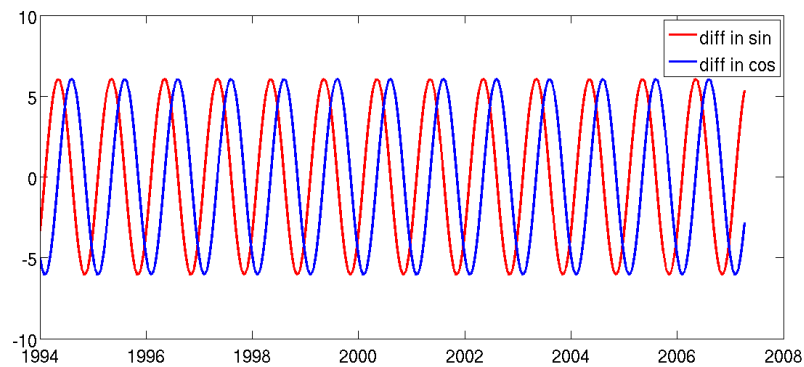
For each day: fit by LSE retrograde diurnal wave

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Time series of differences ((1) - (2)) of estimated amplitudes of sine and cosine for retrograde diurnal wave

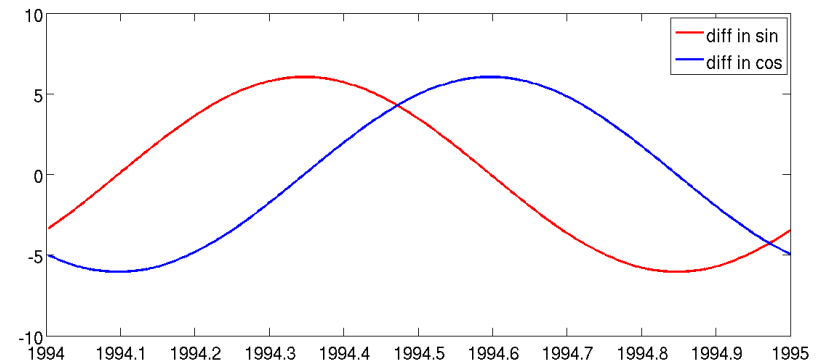
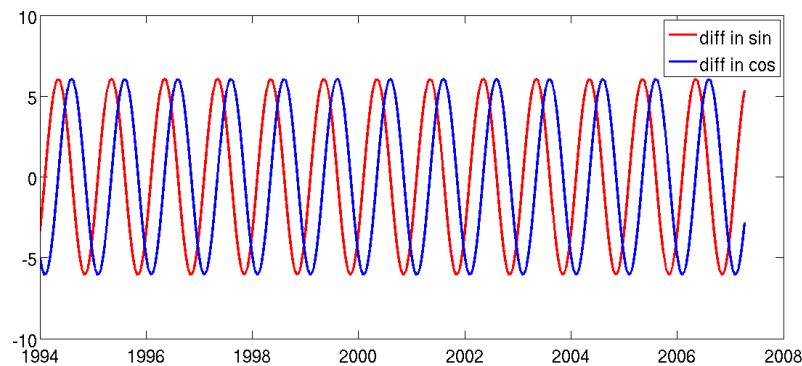
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Differences in amplitudes of sine and cosine for retrograde diurnal wave:  
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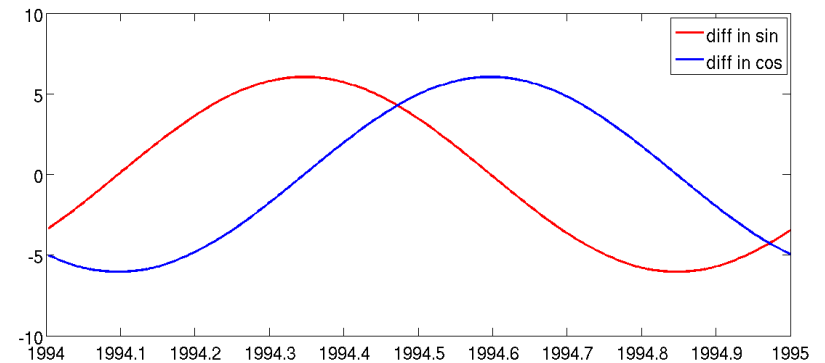
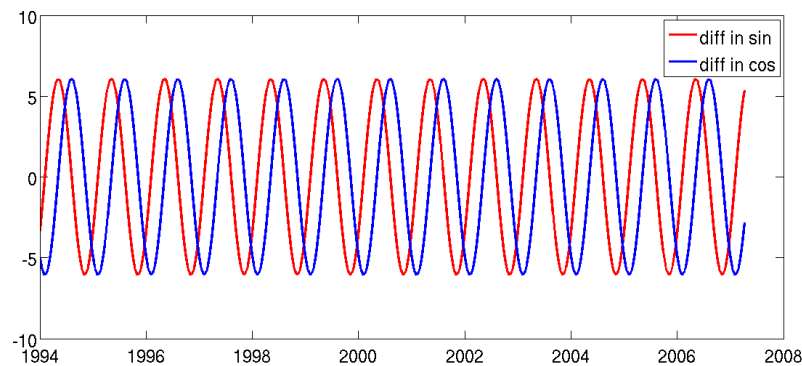
Connection between retrograde diurnal signal in PM and nutation offsets  $\Delta\Psi$ ,  $\Delta\epsilon$ :

$$x_P(t) = -\Delta\psi(t) \cdot \sin\epsilon_0 \cdot \cos\theta - \Delta\epsilon(t) \cdot \sin\theta$$

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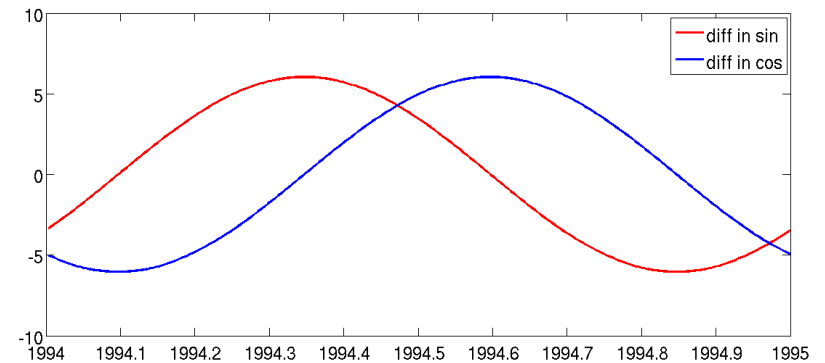
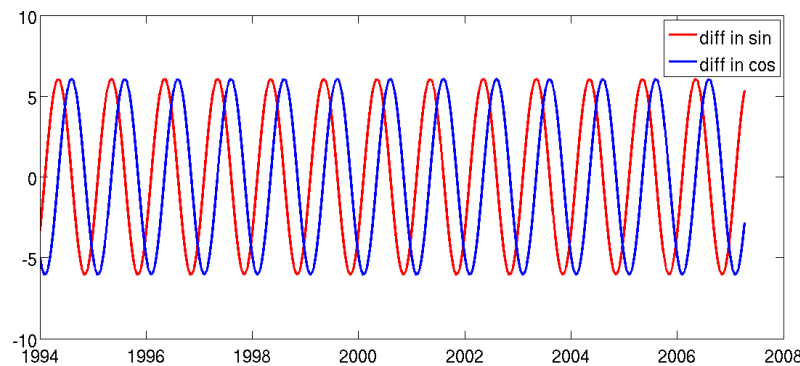
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Differences in amplitudes of sine and cosine for retrograde diurnal wave:  
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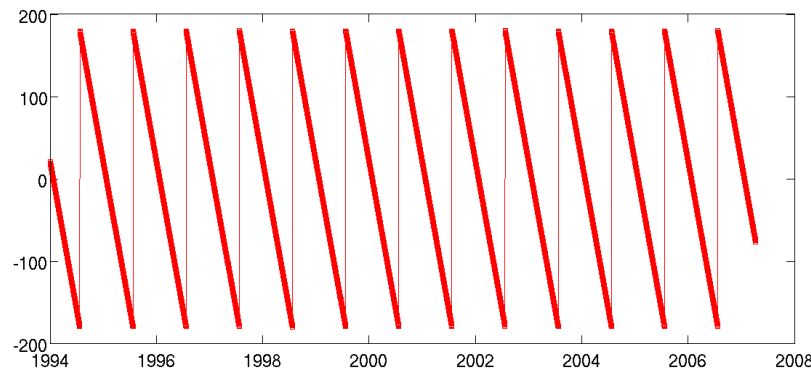
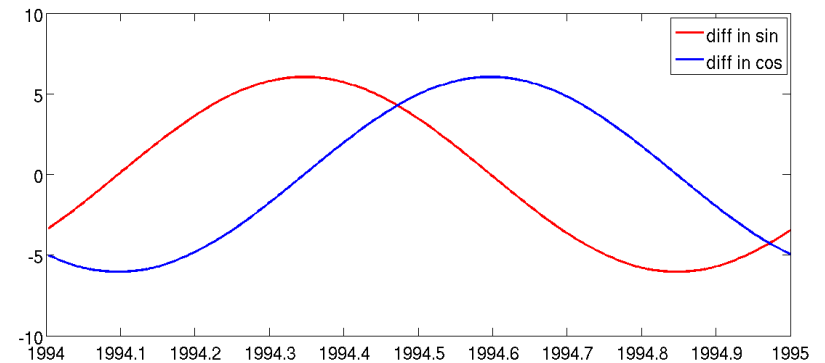
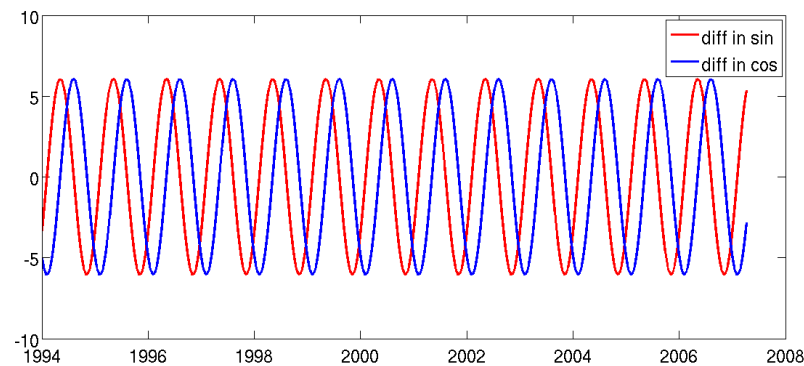
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Corresponds to a relative nutation with a constant offset and period of ~365 days

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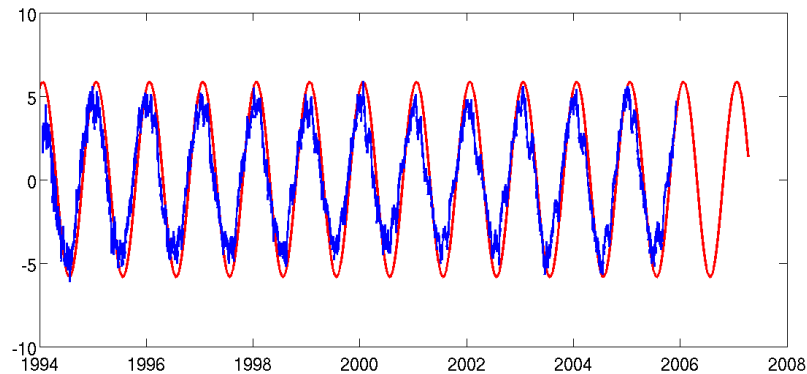


Constant offset, phase period  $\sim 365$  days

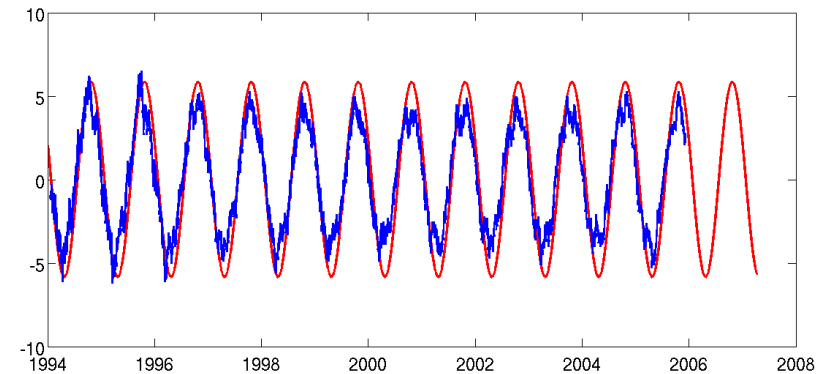
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Differences in amplitudes of sine and cosine for retrograde diurnal wave:  
standard model minus model with changed S1 tide



X-rotation  
Difference in sine amplitudes



minus Y-rotation  
Difference in cosine amplitudes

Corresponds to a relative nutation with a constant offset and period of ~365 days



# (Fictional) Retrograde diurnal signal in subdaily ERPs

Fit retrograde wave over longer time spans:

Better decorrelation from prograde signal

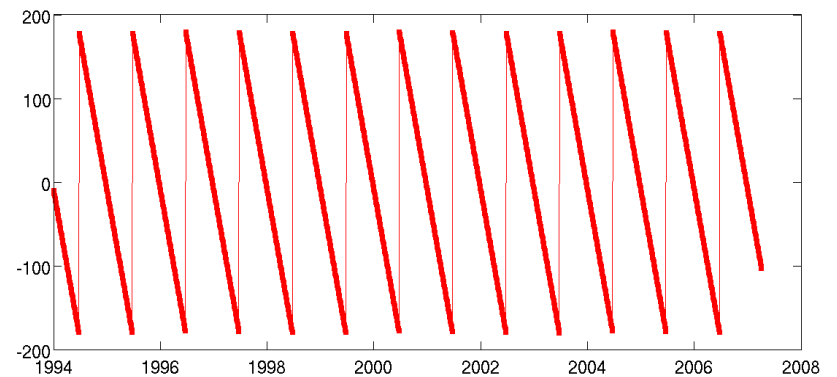
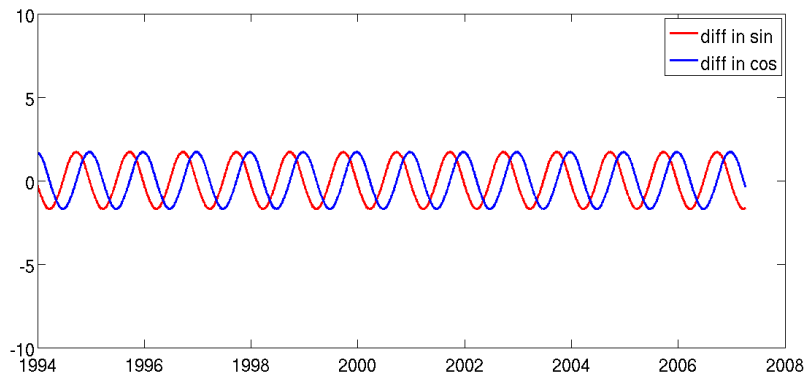
Smaller amplitudes

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Fit retrograde wave over 3 days

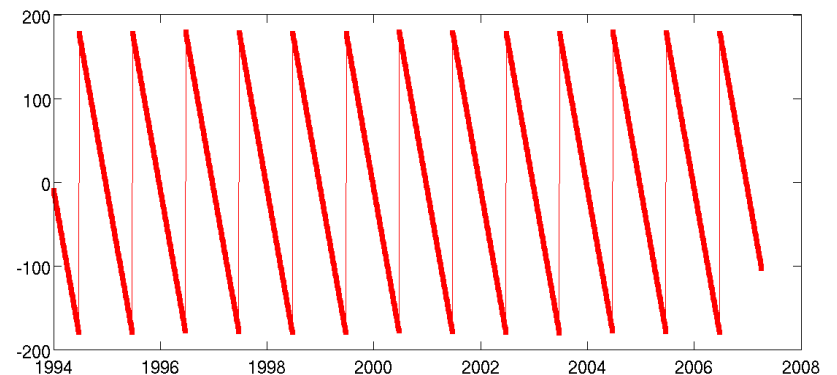
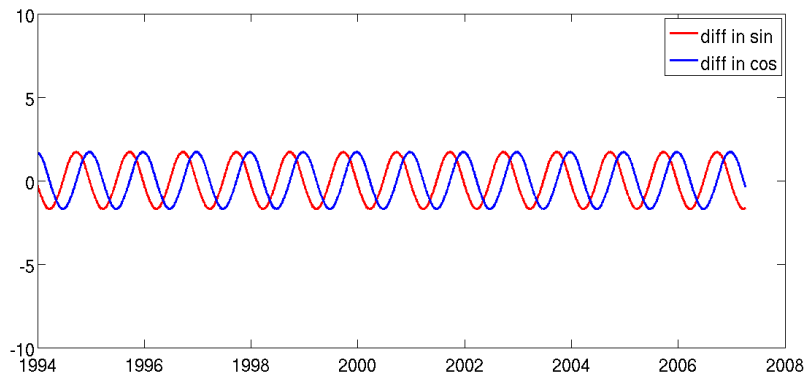


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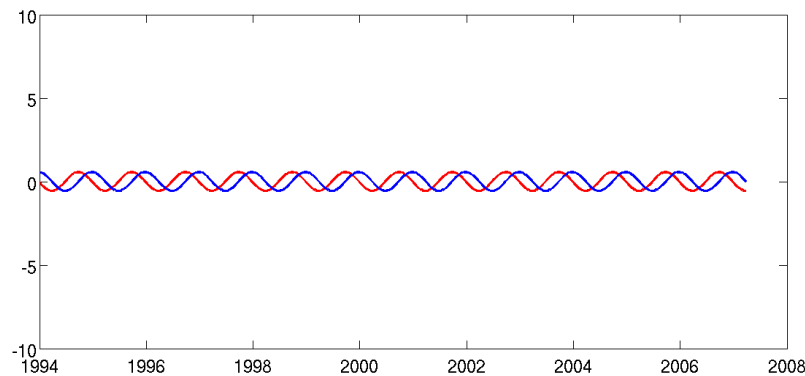
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Fit retrograde wave over 3 days



Fit retrograde wave over 10 days



# Summary and Conclusions

For a 1-day GPS solution:

Part of the diurnal prograde signal in subdaily model for ERPs is mistaken for a retrograde signal

Changes in nutation and orbit orientation

Changes in the orientation of the dynamic reference frame realized by the orbits

Respective periodic signals in time series of orbital parameters, station coordinates and ERPs

Independent of the satellite system used → can be checked with GLONASS

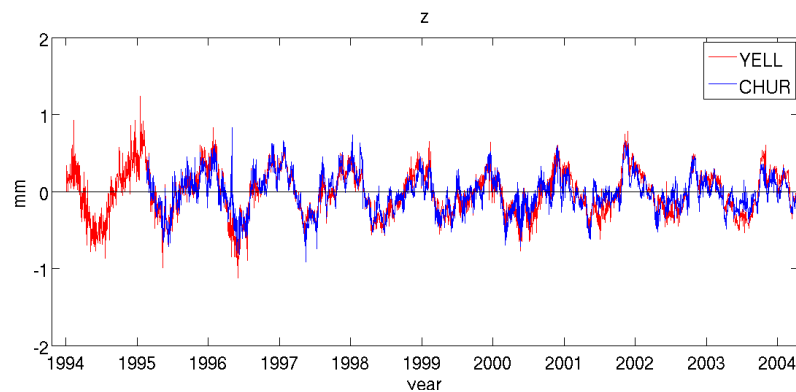
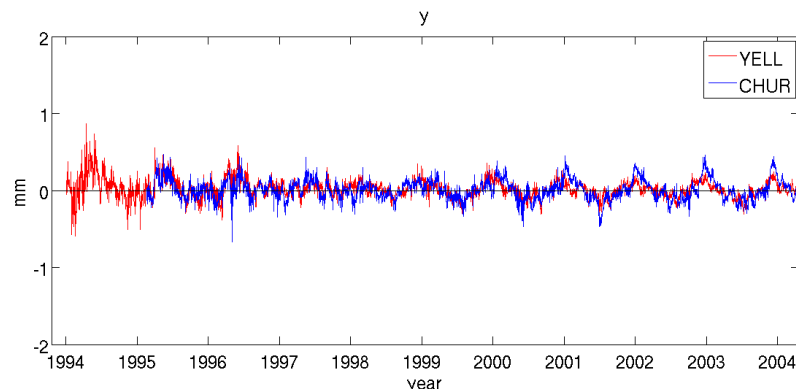
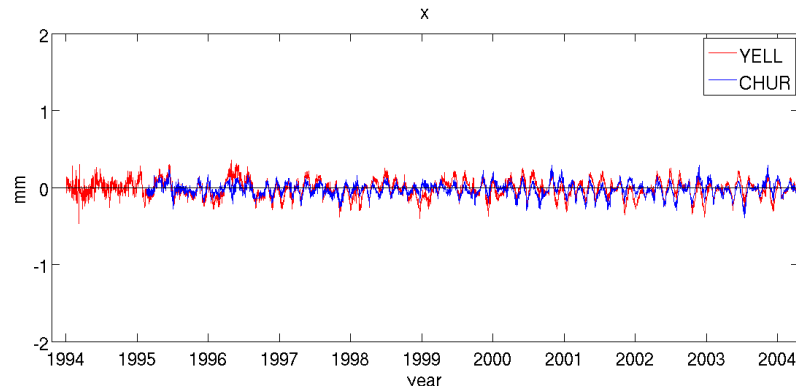
Solution: longer arc length?

estimation of subdaily ERPs?

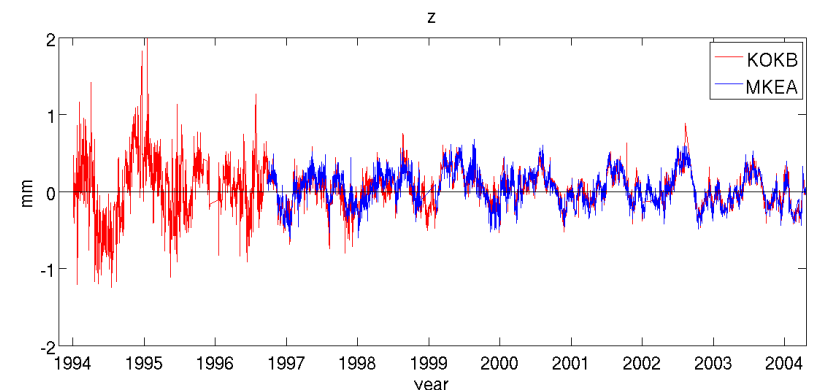
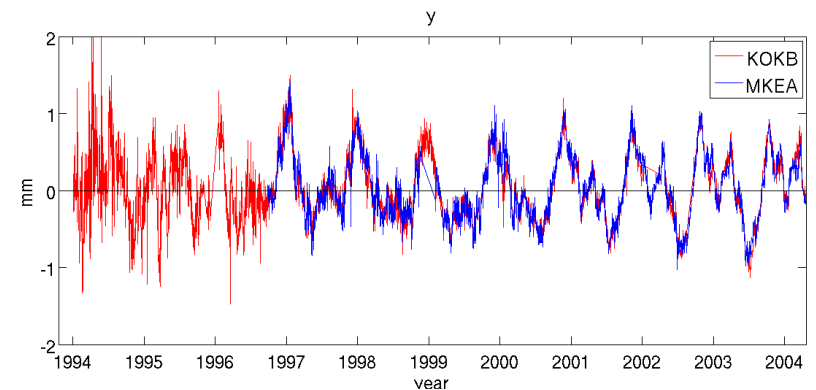
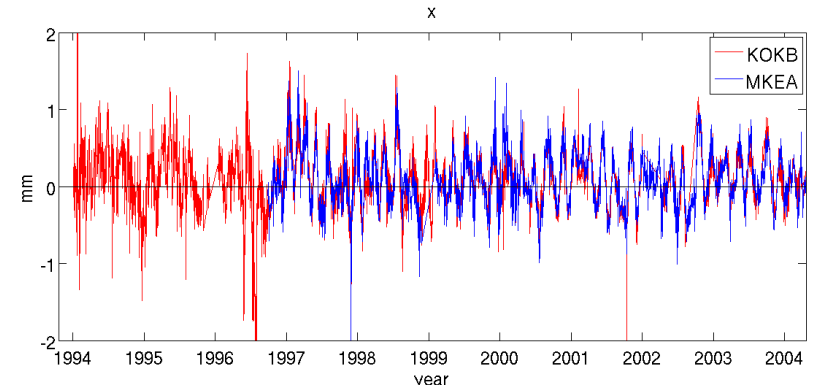
Thank you!

# Influence of tidal model on the station coordinates

## YELL, CHUR (Canada): tide S1



## KOKB, MKEA (Hawaii): tide S1



# Influence of tidal model on the orbit: Kepler elements and radiation pressure parameters

