

# Non-tidal atmospheric loading corrections in global reference frame computations - A case study using SLR -

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# Motivation I

- DFG Research Unit “Reference Systems” (FOR 1503)
 

FOR 1503 comprises a joint project of DGFI and BKG which investigates non-linear station motions based on an extended parameterization (sine-/cosine-terms with periods of 0.5/1yr) and on **different geophysical fluid models**.

	Deformation			Gravity		
	Atmo.	Ocean	Hydro.	Atmo.	Ocean	Hydro.
GGFC	X	X	X	-	-	-
NASA	X	X	X	-	-	-
TU Vienna	X	-	-	X	-	-
Uni Strasburg	X / X	-	X	X	-	X
GFZ	(X)	(X)	(X)	X	X	(X)

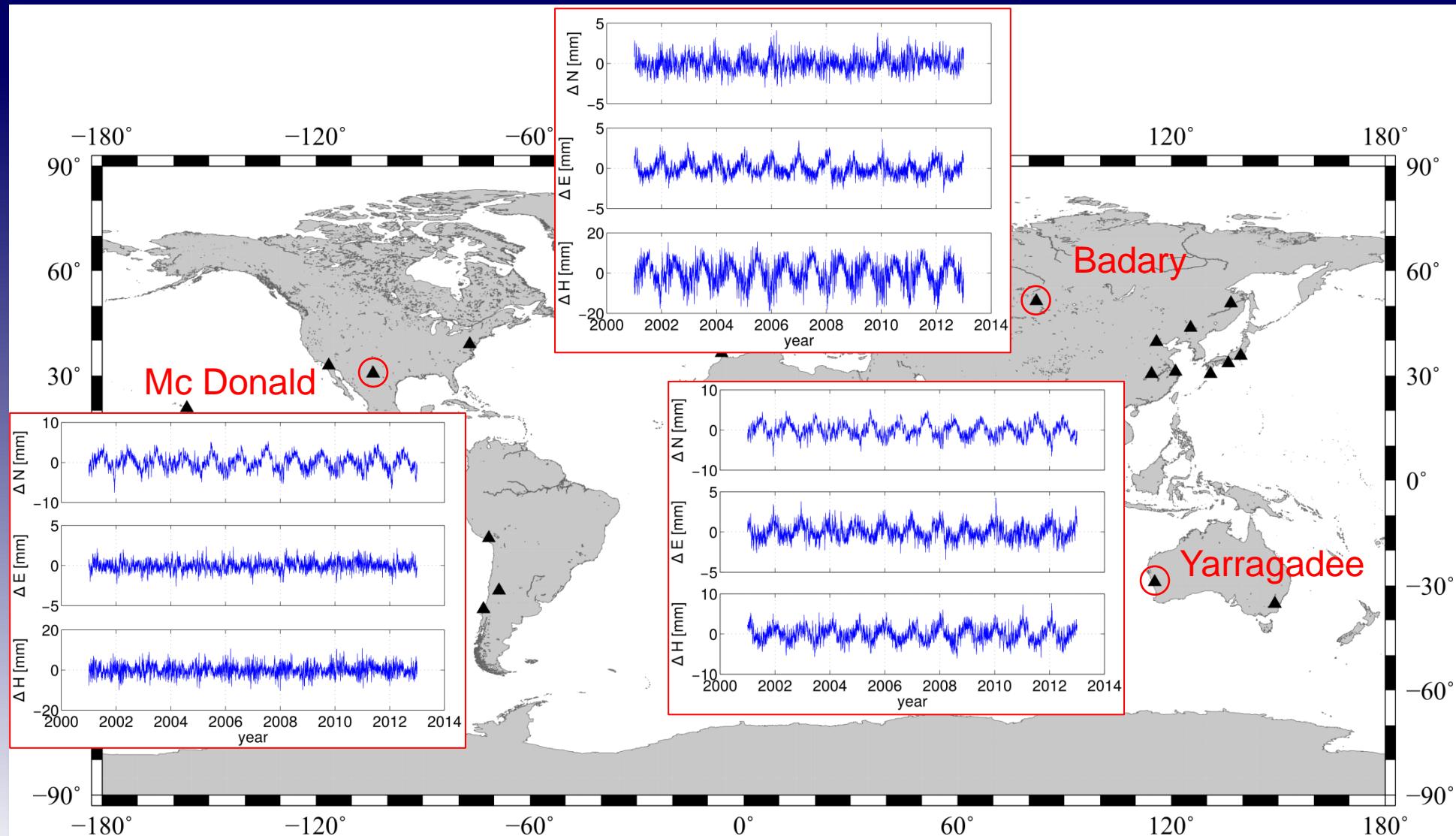
- In this presentation, the non-tidal atmospheric loading (NT-ATML) **site displacement model of NASA** and **gravitational perturbation model of GFZ** will be investigated.

# Motivation II

Furthermore,

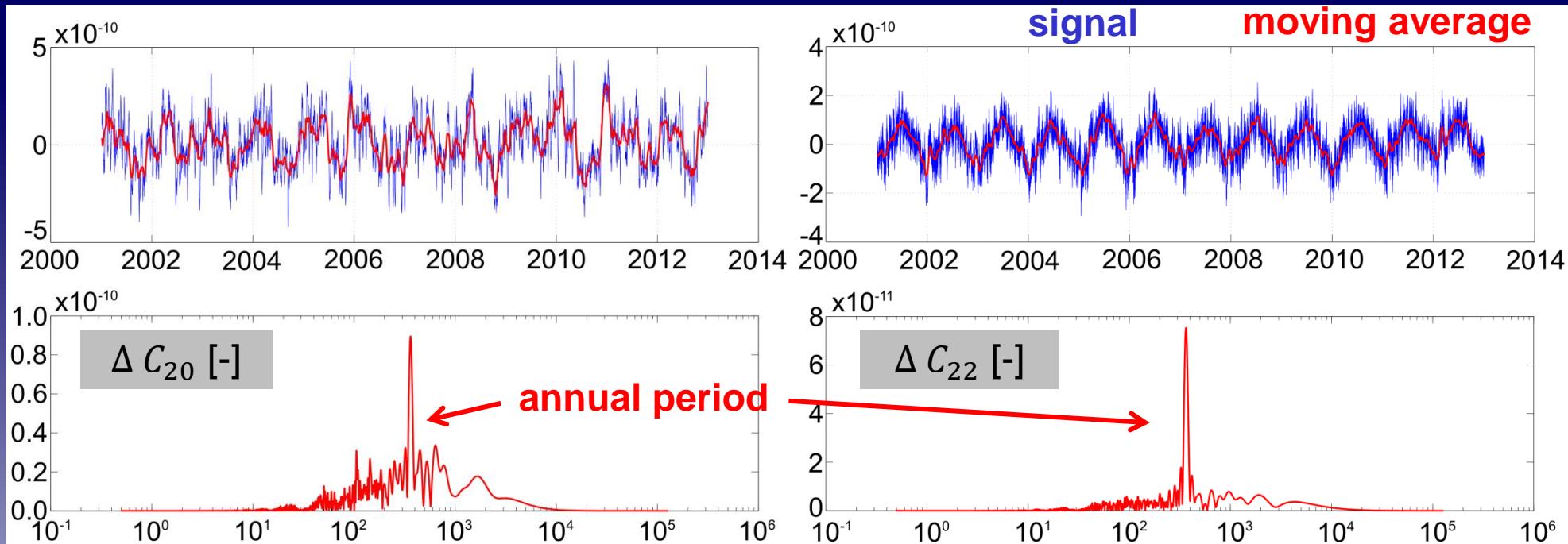
- Unified Analysis Workshop 2011 → ILRS Pilot Project 2012  
*Call for space geodetic solutions corrected for **non-tidal atmospheric loading (site displacement and gravitational perturbation)** at the **observation level**.*
  - ITRF2013 Call for Participation (CfP)  
*“... the **individual TC solutions will be corrected for non-tidal atmospheric loading during the ITRF computation**, using a unique loading model provided by the IERS Global Geophysical Fluid Center (GGFC).”*  
*This correction will be applied at the **normal equation / parameter level**.*
- What is the impact of the NT-ATML corrections on geodetic parameters?
- Does the application at different levels cause any inconsistencies?

# Site displacements due to NT-ATML



The NT-ATML corrections of more than 50% of the SLR stations have an annual amplitude larger than 2 mm in the height component.

# Gravitational perturbation due to NT-ATML



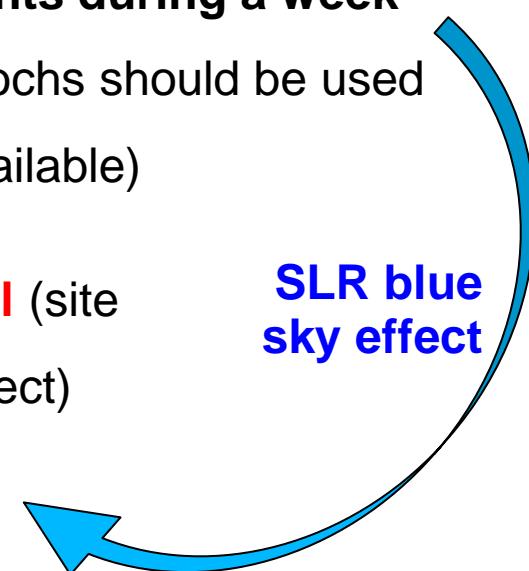
- NT-ATML corrections comprise annual periods with significant amplitudes
- These corrections are only important for geodetic space techniques which observe LEOs/MEOs such as SLR, DORIS (altitude of GNSS satellites is too high)

coefficient	$C_{20}$	$C_{21}$	$S_{21}$	$C_{22}$	$S_{22}$
ampl. (1 yr)	8.95E-11	5.29E-11	1.22E-10	7.54E-11	4.07E-11

# Global reference frame solutions

In order to quantify impact of NT-ATML on global reference frames and EOP, **three test solutions** using SLR data are computed:

- conventional TRF; **no NT-ATML corrections applied**
- TRF + **NT-ATML corrections applied a posteriori** (only site displacements at normal equation / parameter level)
  - **site displacements are a mean of all displacements during a week**
  - consequently only displacements at observation epochs should be used  
(for ITRF2013 processing, this information is not available)
- TRF + **NT-ATML corrections applied at observation level** (site displacements + gravitational perturbations → complete effect)
  - **corrections are applied at observation epochs**



SLR blue sky effect

# Solution setup

The computed global TRFs ...

- contain observations to LAGEOS 1/2 and Etalon 1/2 (weighted by iterative VCE),
- are computed for a time interval between 2001.0 and 2013.0,
- contain station coordinates, velocities (60 stations → 360 parameters),
- contain daily EOP values (terrestrial pole coordinates; 13128 parameters),
- have an orientation realized through an NNR condition w.r.t. a selected subnet of the SLRF2008 (updated),
- contain reduced orbit parameters and station-dependent biases.

# NT-ATML corrections at normal equation level

NT-ATML corrections  $\delta\hat{x}$   
computed from NASA model

SLR-only normal equations

$$\begin{aligned}\tilde{x} &= \hat{x} + \delta x \\ \tilde{x}_0 + \Delta\tilde{x} &= x_0 + \Delta\hat{x} + \delta x\end{aligned}$$

Keeping the a priori values ( $\tilde{x}_0 = x_0$ ) yields

$$\begin{aligned}\Delta\tilde{x} &= \Delta\hat{x} + \delta x \\ \Delta\tilde{x} &= N^{-1}(y + N\delta x) = N^{-1}\tilde{y}.\end{aligned}$$

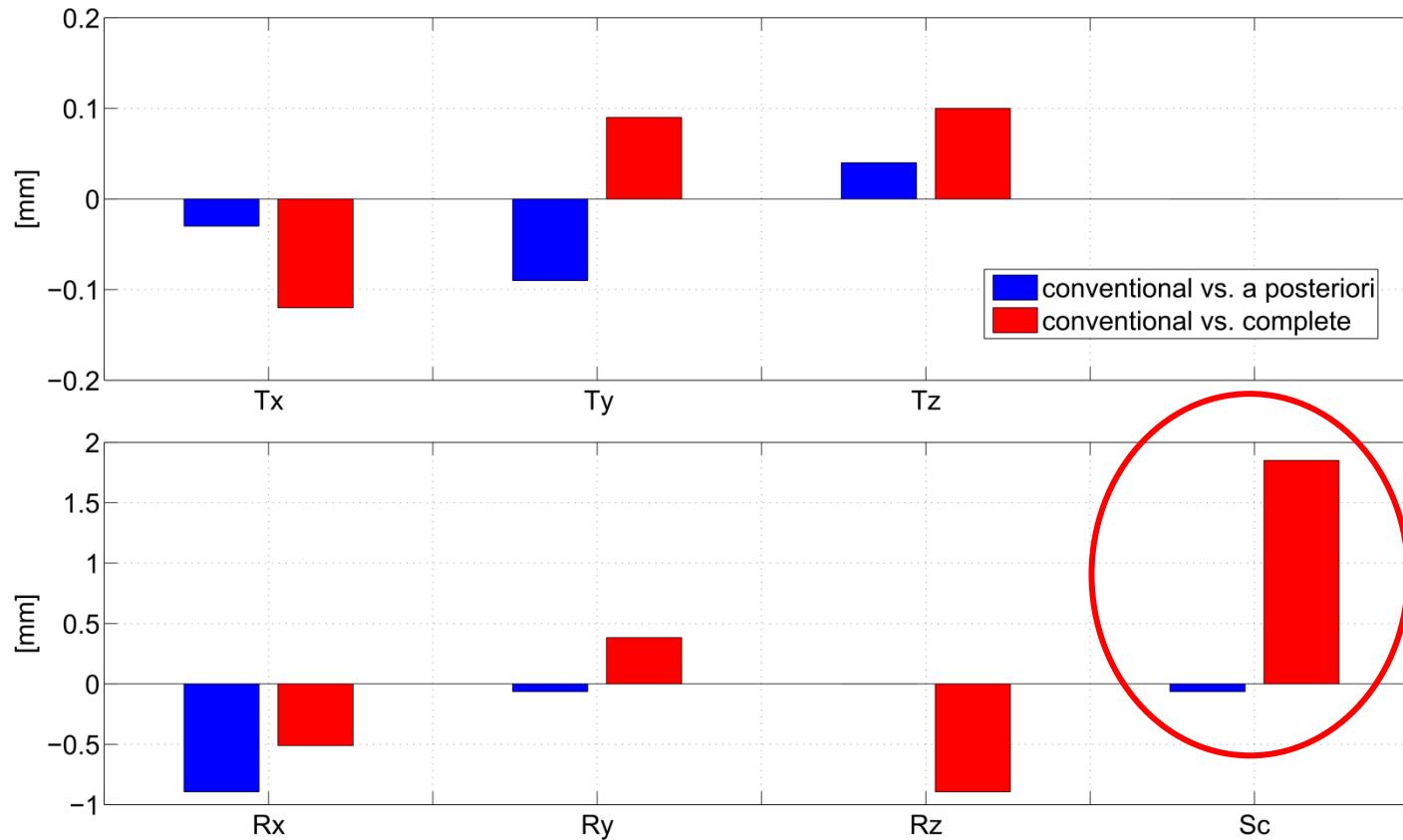
SLR-only normal equations  
corrected a posteriori for  
NT-ATML



$$\begin{aligned}\tilde{N} &= N, \\ \tilde{y} &= y + N\delta x, \\ \tilde{l}^T \tilde{P}_{ll} \tilde{l} &= l^T P_{ll} l + \delta x^T (2y + N\delta x), \\ \tilde{x}_0 &= x_0.\end{aligned}$$

- Accumulation ...
- Introduction of station velocities ...
- Realization of geodetic datum ...

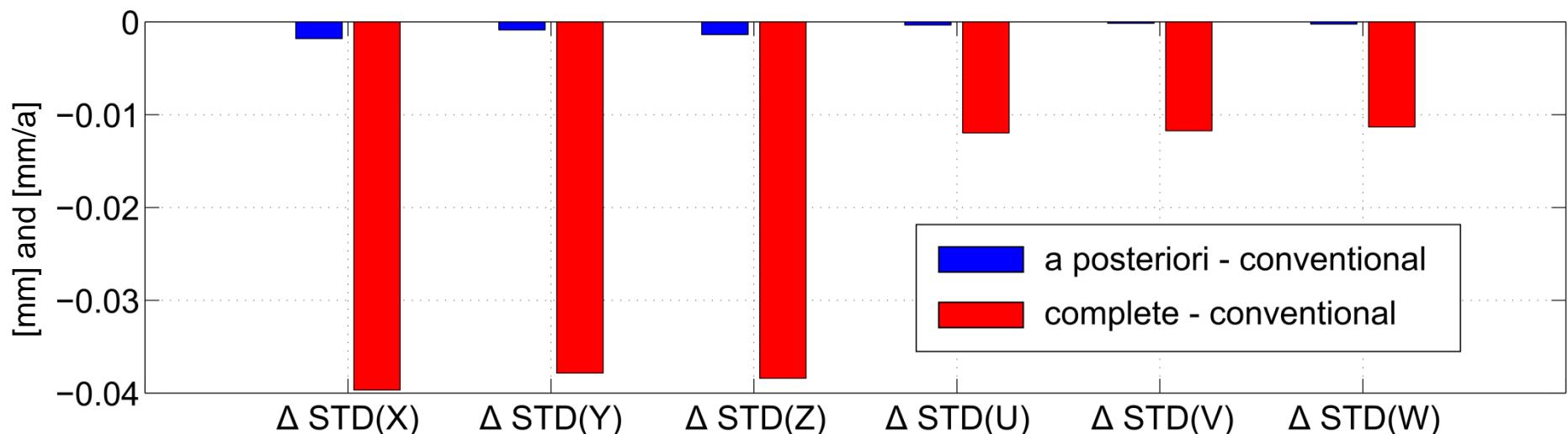
# Impact on geodetic datum of global TRFs



- Translations are very small (< 0.20 mm), rotations are smaller than 1.0 mm
- Different treatment of NT-ATML corrections cause scale difference of ca. 1.8 mm (this might be caused by gravitational perturbation and blue sky effect)
- Rates are nearly zero for all parameters

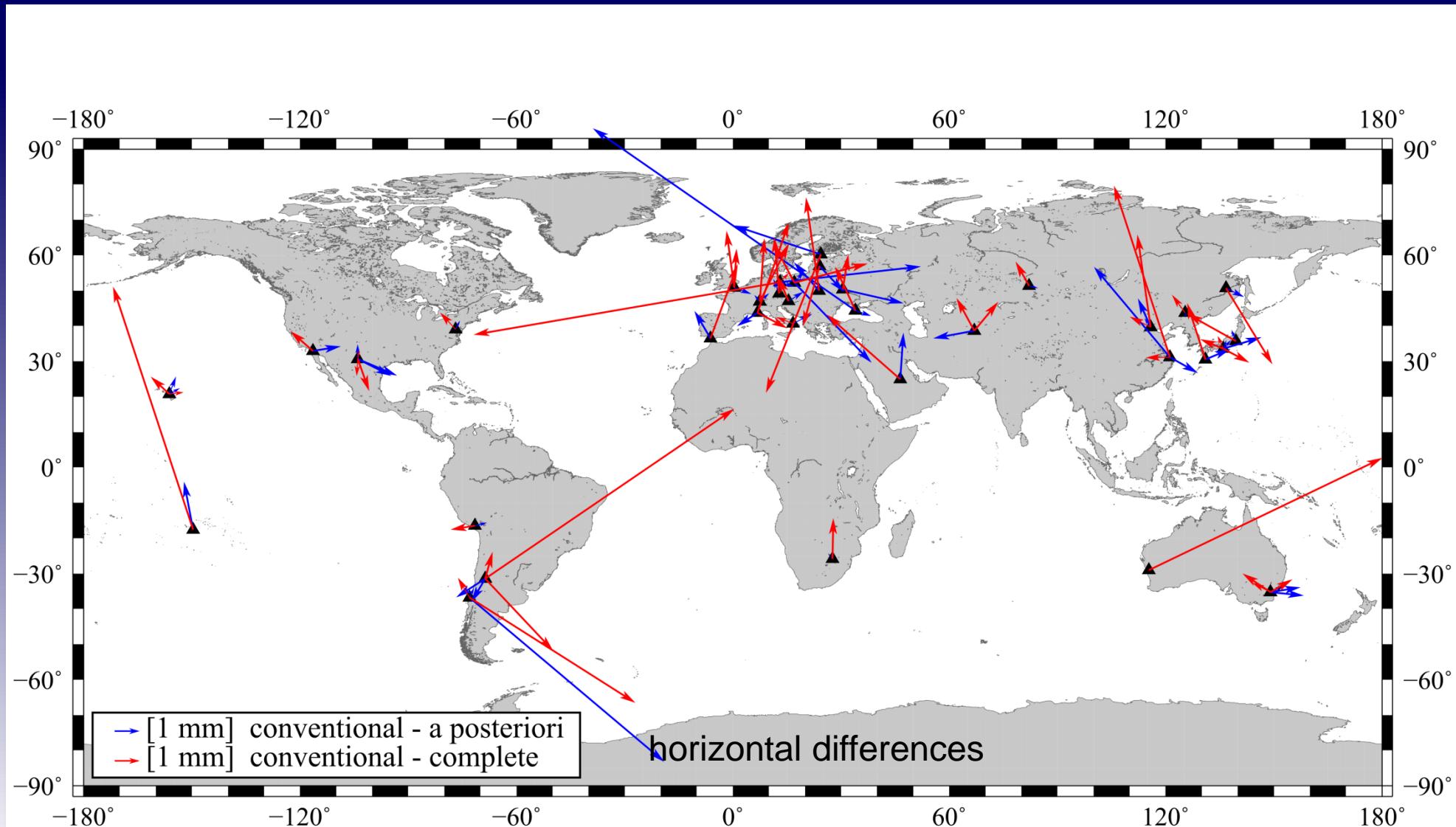
# Impact on internal accuracy of TRFs

	$l^T P l$	$\hat{v}^T P \hat{v}$
conventional TRF	5.16656E+06	3.09233E+06
a posteriori corr. TRF	5.17203E+06	3.09861E+06
complete corr. TRF	5.12014E+06	2.98952E+06

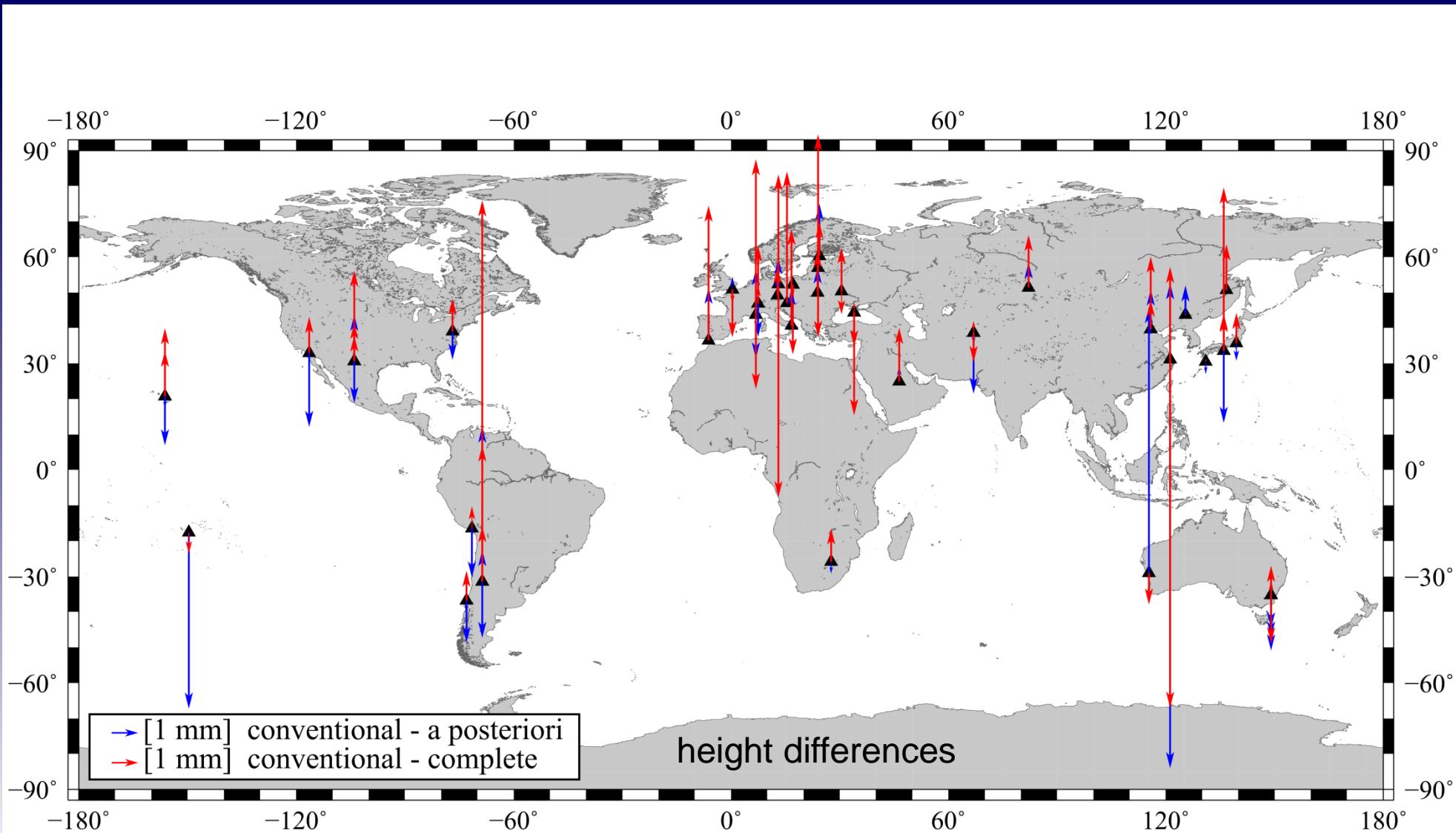


- $l^T P_{ll} l$  and  $\hat{v}^T P_{ll} \hat{v}$  are dominated by the EOP (13128 EOP vs. 360 station parameters)
- differences in the coordinate / velocity STDs are very small (<0.05 mm)

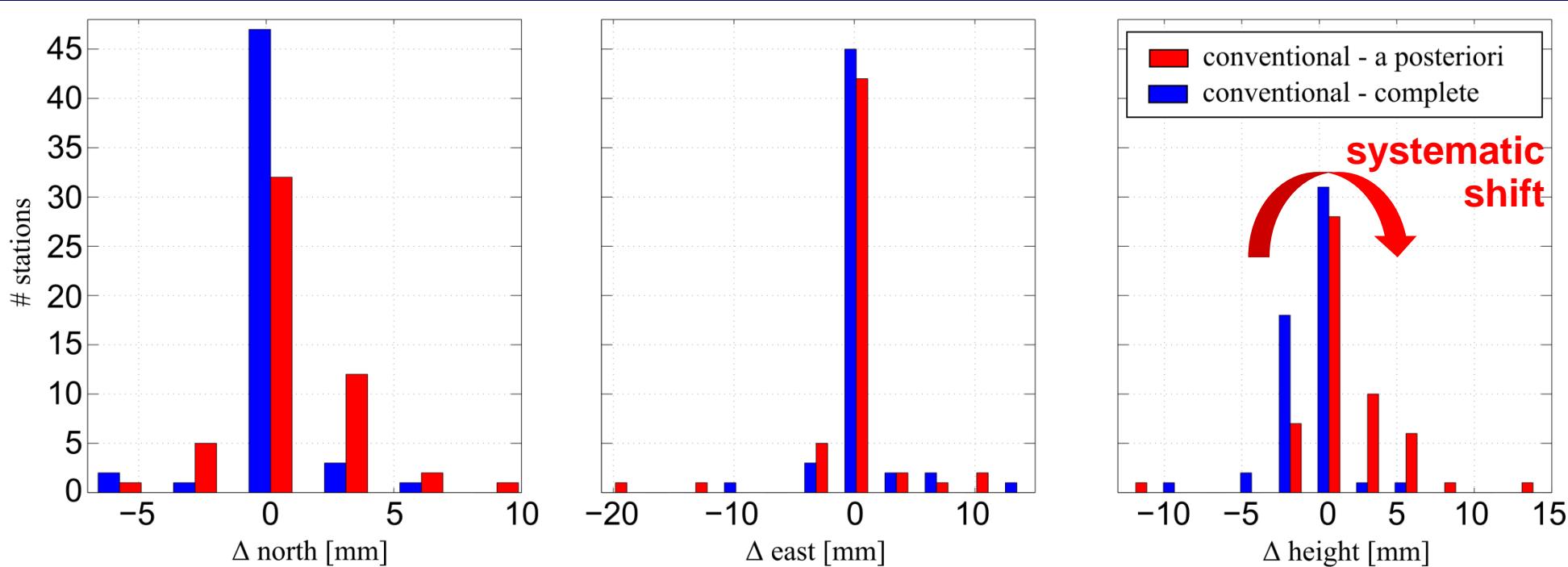
# Impact on station coordinates / velocities I



# Impact on station coordinates / velocities II

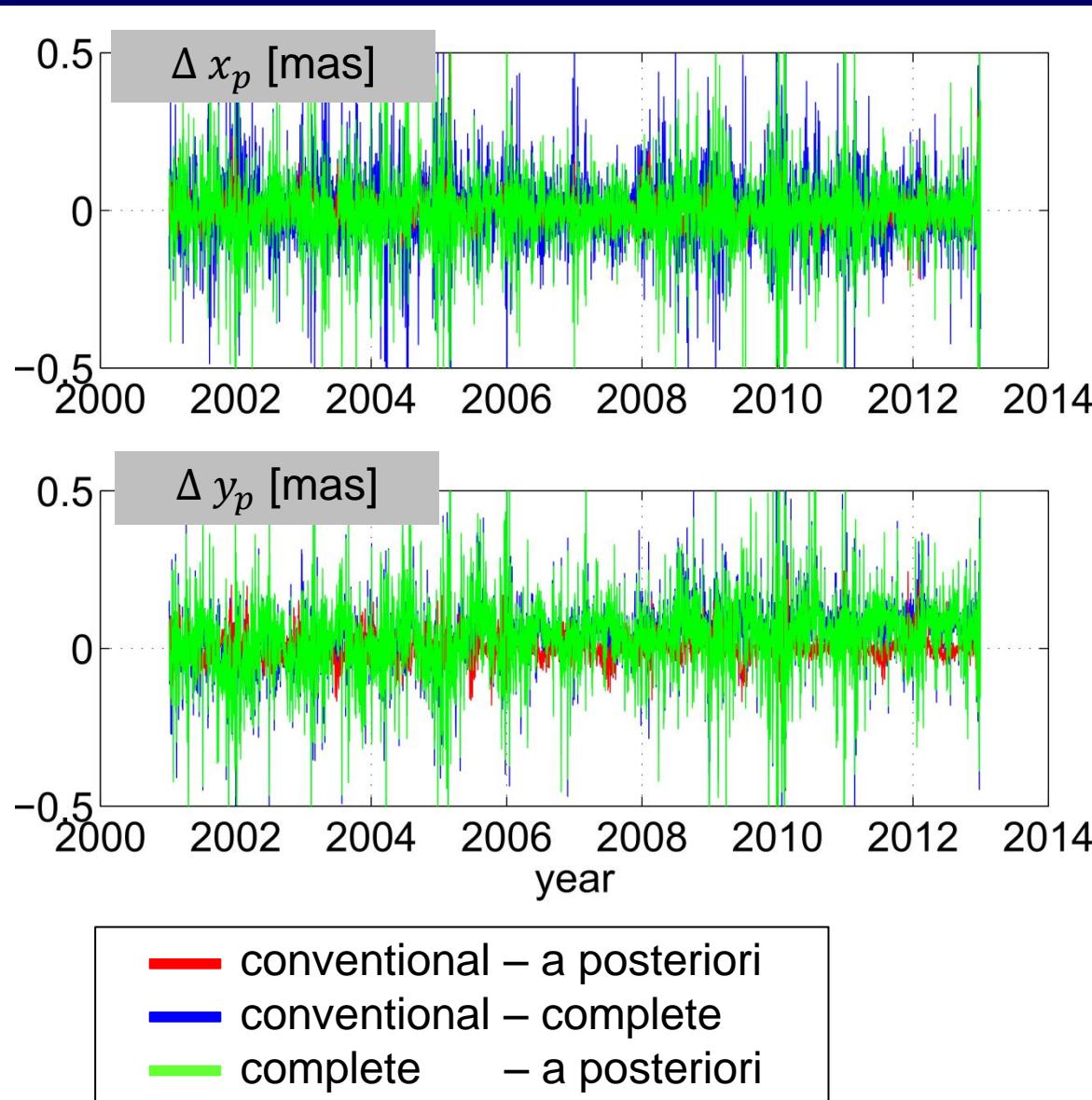


# Impact on station coordinates / velocities III



- horizontal coordinate differences show no systematic change between a posteriori and complete correction
- height differences show a **systematic shift into positive domain in the southern and northern hemisphere**  
→ scale factor!

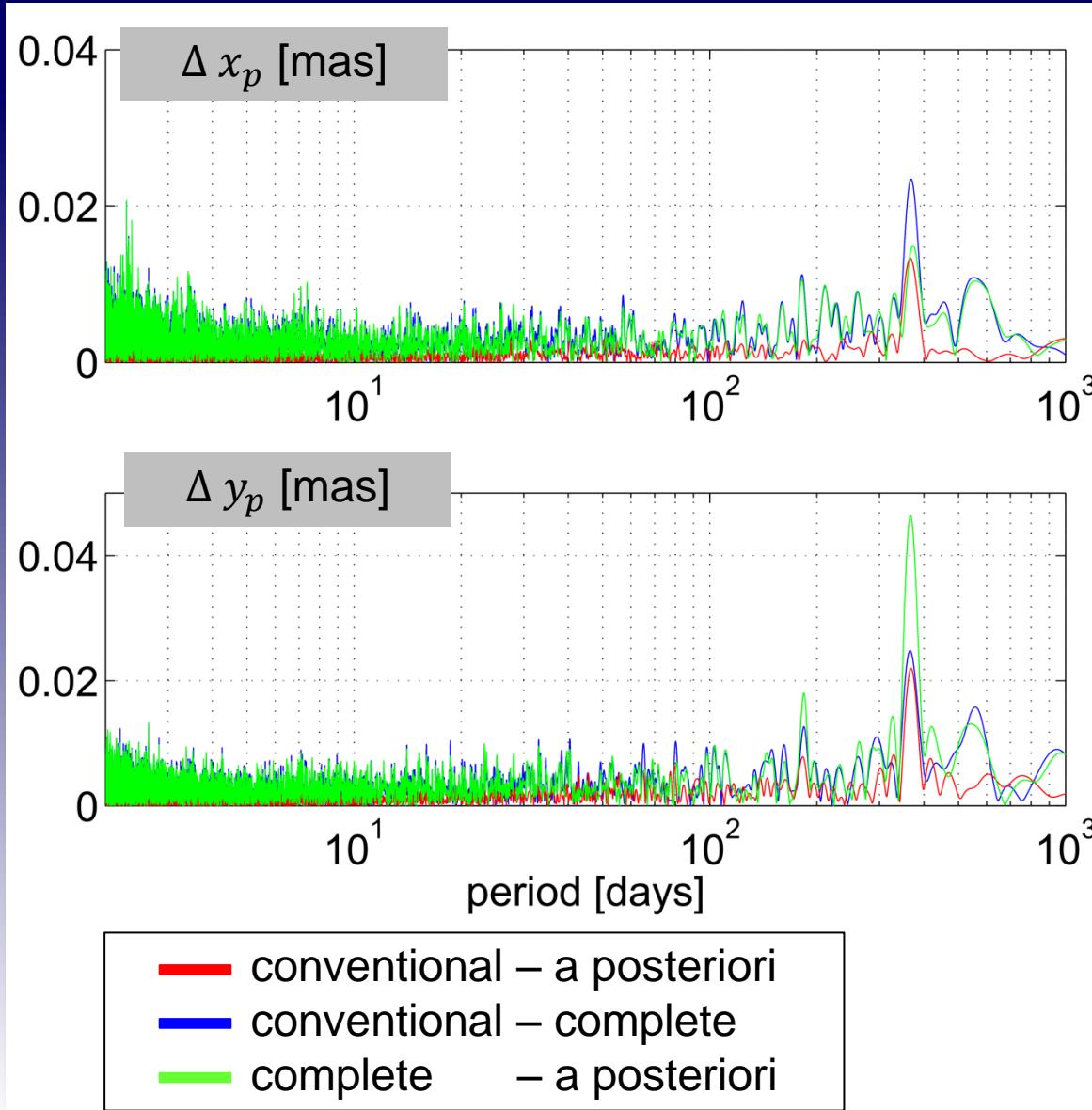
# Impact on terrestrial pole coordinates I



- $\Delta x_p$  time series agree well w.r.t. each other
- $\Delta y_p$  time series of a posteriori and complete corrected TRF show small systematic drift w.r.t conventional TRF
- Improvement of STDs:

$\Delta \text{STD}(x_p)$	$\Delta \text{STD}(y_p)$
<b>0.18 <math>\mu\text{s}</math></b>	<b>3.4 <math>\mu\text{s}</math></b>
<b>0.17 <math>\mu\text{s}</math></b>	<b>3.4 <math>\mu\text{s}</math></b>

# Impact on terrestrial pole coordinates II



□ Application of NT-ATML corrections at different levels cause differences in polar motion with clear seasonal variations

□  $\Delta x_p$

amplitude [mas]	phase [deg]
<b>0.014 ± 0.001</b>	<b>93.6 ± 3.3</b>
<b>0.023 ± 0.004</b>	<b>63.9 ± 3.0</b>
<b>0.015 ± 0.004</b>	<b>32.5 ± 3.2</b>

□  $\Delta y_p$

amplitude [mas]	phase [deg]
<b>0.023 ± 0.001</b>	<b>102.3 ± 2.7</b>
<b>0.027 ± 0.003</b>	<b>270.3 ± 5.6</b>
<b>0.047 ± 0.002</b>	<b>96.8 ± 3.5</b>

# Summary

The application of the **gravitational perturbation** is only necessary for LEOs/MEOs  
(→ correction only important for DORIS and SLR)

The different applications of NT-ATML corrections

- at observation equation level (**site displacement + gravitational perturbation at observation epoch**) and
- at normal equation / parameter level (**only weekly mean site displacement**) cause

- a **difference of ca. 1.8 mm in the scale** between the a posteriori corrected TRF and the complete corrected TRF (SLR blue sky effect)
- an **small improvement in the stochastic model** (improved STDs) if the complete correction is applied at the observation equation level
- **systematic differences with annual period in the terrestrial pole coordinates** (different amplitudes in  $x_p$ ,  $y_p$  and a phase shift of ca. 180 degree in  $y_p$ )

# Outlook

## Future investigations:

- Separation of **SLR blue sky effect, effect due to gravitational perturbation and effect of the application at different levels**
- Evaluation of other model combinations (currently NASA and GFZ have been used)
- Investigation of the hydrological and oceanic non-tidal loading (site displacement and gravitational perturbation)
- Application of non-tidal corrections to DORIS

## For ITRF2013 computation:

- GGFC NT-ATML model will be used for ITRF2013 computation
- Further investigation of NT-ATML effect on station coordinates/velocities
- Investigation if combined pole coordinates are affected

# Thank you very much for your attention!

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